



ELSEVIER

Available at  
www.ComputerScienceWeb.com  
POWERED BY SCIENCE @ DIRECT®

COMPUTER  
NETWORKS

Computer Networks 43 (2003) 211–226

www.elsevier.com/locate/comnet

# Modeling web requests: a multifractal approach

Abdullah Balamash, Marwan Krunz \*

*Department of Electrical and Computer Engineering, College of Engineering and Mines, University of Arizona,  
1230 E. Speedway Blvd., Tucson, AZ 85721-0104, USA*

Received 3 September 2002; received in revised form 14 March 2003; accepted 17 March 2003

Responsible Editor: N.L.S. Fonseca

---

## Abstract

World Wide Web (WWW) caching is used to improve network latency and bandwidth usage by storing previously requested files in a cache. Ideally, the cache replacement policy should account for the intrinsic characteristics of WWW traffic, which include temporal locality, spatial locality, and popularity. In this paper, we accurately capture these three characteristics in a stochastic model, which can be used to generate synthetic WWW traces and assess WWW cache designs. To capture temporal and spatial localities, we use a modified version of Riedi et al.'s multifractal model, where we reduce the complexity of the original model from  $\mathcal{O}(N)$  to  $\mathcal{O}(1)$ ;  $N$  being the length of the synthetic trace. Our model has the attractiveness of being parsimonious (characterized by few parameters) and that it avoids the need to apply a transformation to a self-similar model (as often done in previously proposed models), thus retaining the temporal locality of the fitted traffic. Furthermore, because of the scale-dependent nature of multifractal processes, the proposed model is more flexible than monofractal (self-similar) models in describing irregularities in the traffic. Trace-driven simulations are used to demonstrate the goodness of the proposed model in terms of generating representative WWW streams and approximating the cache performance of actual WWW traffic.

© 2003 Elsevier B.V. All rights reserved.

*Keywords:* WWW modeling; Web caching; Multifractals; Stack distance; Self-similarity

---

## 1. Introduction

As the World Wide Web (WWW) continues to grow at an astounding rate, its clients are experiencing excessive response times and its servers are frequently stretched to their capacity limits. One way to deal with this problem is to use WWW caching. Caches are placed either in the proximity

of clients to reduce their perceived latency or close to servers to reduce their loads. To be of any practical benefit, the cache should only store the most popular documents. Determining which documents are important and which ones are to be flushed out in case of cache saturation is the primary function of a cache replacement policy. An ideal replacement policy tries to take into account the intrinsic properties of WWW traffic in its design. These properties include temporal locality, spatial locality, and popularity. Temporal locality measures the closeness in time between requests to the same document. Spatial locality measures the

---

\* Corresponding author.

*E-mail addresses:* [balamash@ece.arizona.edu](mailto:balamash@ece.arizona.edu) (A. Balamash), [krunz@ece.arizona.edu](mailto:krunz@ece.arizona.edu) (M. Krunz).

correlation between requests to different documents (e.g., if document  $A$  is currently being requested, then there is a good chance that document  $B$  will be requested in the near future). Popularity refers to the overall likelihood of requesting a particular document, independent of other documents.

The ability to assess the performance of WWW caching policies hinges on the availability of representative workload that can be used in trace-driven simulations [4,13]. Measured (“real”) traces can be used for this purpose. However, due to the difficulty associated with capturing real traces, only a handful of such traces are available in the public domain (see [19] for public domain traces). This makes it hard to provide simulation results with reasonable statistical credibility. A more feasible alternative is to rely on synthetic traces that are derived from an approximate stochastic model. The need for such a model is the main motivation behind our work.

In this paper, we present a modified version of Riedi et al.’s multifractal model [17]. We use this modified version to simultaneously capture the temporal and spatial localities of WWW traffic. Riedi’s model has the attractiveness of being able to simultaneously approximate the (lognormal) marginal distribution and the correlation structure of the traffic. Its main disadvantage is its complexity, which grows linearly with the size of the generated trace. We modify this model, reducing its complexity to  $\mathcal{O}(1)$ . The resulting model is parsimonious in that it is characterized by four to five parameters representing the mean, variance, and correlation structure of the “normalized stack distance” string (explained below). The popularity profile of the traffic is incorporated in the model during the trace generation phase, assuming that the popularity profiles for all documents are given beforehand. Our model is mainly intended for offline generation of the traffic demand *seen by a WWW server*. Accordingly, the popularity profiles can be easily computed from the server logs.

The rest of the paper is organized as follows. Section 2 describes the related work. In Section 3 we describe the data sets used in our study. In Section 4 we give a brief overview of Riedi et al.’s multifractal model and the modification we make

to it to render it parsimonious. The proposed WWW traffic generation approach is given in Section 5, followed by simulation studies in Section 6. We conclude the paper in Section 7.

## 2. Related work

WWW traffic modeling has been the focus of several previous studies; examples of which are given in [1,3,7,14,15]. In these studies, the temporal locality of the traffic was represented by the marginal distribution of the stack distance string. This distribution was found to follow a lognormal-like shape. The stack distance string, which is an equivalent representation of a reference string, is obtained by transforming the reference string using the least recently used (LRU) stack, as follows. Let the reference string be  $R_t = \{r_1, r_2, \dots, r_t\}$ , where  $r_j$  is the document (or object) requested at time  $j$ . Note that a document may appear multiple times in  $R_t$ . Let the LRU stack at time  $t$  be  $S_t = \{Obj_1, Obj_2, Obj_3, \dots, Obj_n\}$ , where  $Obj_1, Obj_2, \dots, Obj_n$  are distinct documents;  $Obj_1$  is the most recently requested document,  $Obj_2$  is the second most recently requested document, and so on. Let  $d_t$  be the stack distance of the document referenced at time  $t$  (the position of the document in the LRU stack at time  $t-1$ ). Whenever a reference is made to a document, the LRU stack must be updated. If  $r_{t+1} = Obj_j$ , then the LRU stack becomes  $S_{t+1} = \{Obj_j, Obj_1, Obj_2, \dots, Obj_{j-1}, Obj_{j+1}, \dots, Obj_n\}$  and  $d_{t+1} = j$ . Thus, for any reference string  $R_t = \{r_1, r_2, \dots, r_t\}$ , there is a corresponding stack distance string  $D_t = \{d_1, d_2, \dots, d_t\}$ .

In [1] the authors showed that spatial locality can be captured (at least, in part) through the autocorrelation structure (ACF) of the stack distance string. They argued that the stack distance string exhibits long-range dependent (LRD) behavior. Thus, to simultaneously model the marginal distribution (temporal locality) and the correlation structure (spatial locality) of the stack distance string, they relied on the work in [12], which proved the invariance of the Hurst parameter to transformations of the marginal distribution of an LRD process. More specifically, the authors in [12] proved that under some mild as-

sumptions, a point-by-point transformation  $Y = F_y^{-1}(F_x(X))$  of a Gaussian self-similar process  $X$  with Hurst parameter  $H$  results in a self-similar process  $Y$  with the same Hurst parameter, where  $F_x$  and  $F_y$  are the CDFs for  $X$  and  $Y$ , respectively. It should be noted, however, that this result is valid asymptotically and only for Gaussian processes (e.g., fractional ARIMA). More importantly, while this result assures the invariance of  $H$ , it does not necessarily preserve the shape of the ACF. As an example, consider the transforming of the Gaussian distribution of a F-ARIMA model into a lognormal distribution, which adequately models the marginal distribution of the stack distance string. The resulting ACFs are shown in Fig. 1, along with the ACF of a real WWW stack distance string. The figure illustrates the two main drawbacks of the transformation. First, while the transformation may capture the asymptotic behavior of the ACF (the  $H$  parameter), it destroys the overall shape of the original ACF of the F-ARIMA model. Second, the original F-ARIMA model itself is not accurate in representing the real ACF at small and moderate lags.

To avoid the problems stated above, we resort to multifractal modeling to simultaneously capture the correlation structure and marginal distribution of the stack distance string. Fig. 2 shows the accuracy of the multifractal model (which we de-

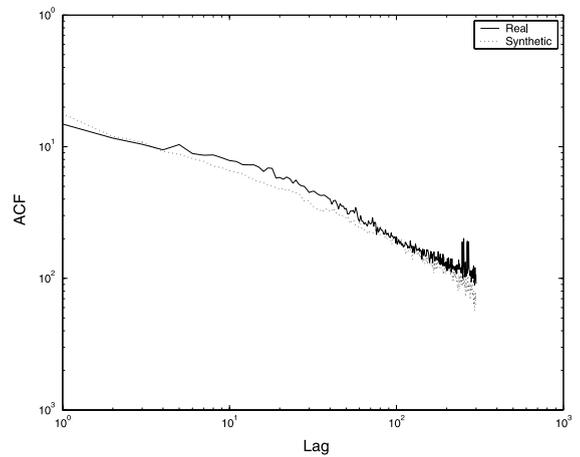


Fig. 2. Accuracy of the multifractal model in capturing the ACF of the stack distance string of a real WWW trace.

scribe in Section 4) in capturing the ACF of the stack distance string of a WWW trace. Multifractality is a generalization of self-similarity (monofractality), whereby the Hurst parameter (the scaling exponent) is not fixed, but varies with scale. This variability makes multifractal processes more flexible than monofractal processes in describing “irregularities” in the traffic (e.g., contrasting short-term and long-term behaviors). The reader is referred to [8–11,17,18] and the references therein for comprehensive discussions of multifractal processes. In [17] the authors used a wavelet-based construction of a multifractal process to show that the correlation behavior of a strongly correlated time series can be approximately captured by appropriately setting the second moments of the wavelet coefficients of the multifractal process. This result provides the basis for modeling the ACF of the stack distance string. Combined with the fact that the above multifractal model exhibits an approximately lognormal marginal distribution, it can be used to model both the temporal and spatial localities in WWW traffic.

In [16], the authors studied the temporal locality in WWW traffic and concluded that such phenomenon is induced by both temporal correlations and long-term popularity. More specifically, references to long-term popular documents tend to be close to each other in time. Moreover, references to certain unpopular documents (in the long term)

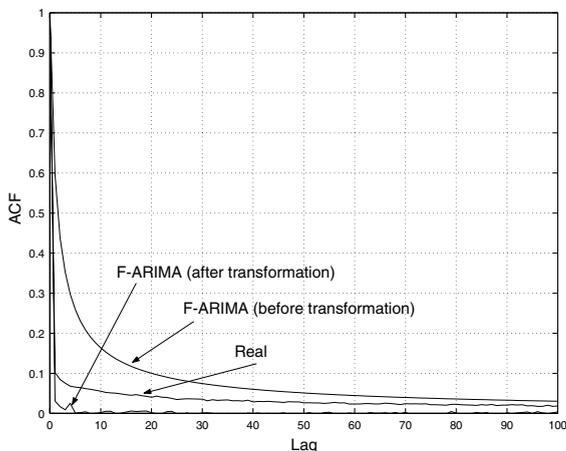


Fig. 1. Impact of transforming the marginal distribution of a F-ARIMA model on the correlation structure.

exhibit strong temporal correlations, as these references appear “clustered” in time (e.g., a document that is extensively requested but only during a short period of time). It is important to differentiate between the two sources of temporal locality [15,16]. The standard stack-distance-string approach does not differentiate between the two, since its distribution is predominantly affected by the popularity profile (i.e., long-term popularity). To address this problem, the authors in [5] introduced a new measure for temporal locality, called the *scaled stack distance*, to deal with this problem. The scaled stack distance string is a normalization of the stack distances by their expected values (assuming that requests to a given document are evenly distributed over the duration of the trace). Measures short-term temporal correlations and is insensitive to long-term popularity, which itself is captured during the trace generation process. For our WWW traffic model, we use the same measure, which we refer to as the *normalized stack distance*. Accordingly, equally popular documents have the same expected stack distance. The normalized stack distance string is found to have a lognormal-like distribution and a slowly decaying correlation structure (i.e., LRD behavior). We employ the multifractal model to capture both the marginal distribution and the correlation structure of the normalized stack distance string. We use extensive simulations to evaluate the performance induced by our WWW traffic model and contrast it with the self-similar model in [1] and the model in [5], using the original (real) traces as a point of reference. Our evaluation measures include sample statistics of the synthetic traces (e.g., mean, variance, correlations, percentiles) as well as the cache

and byte hit ratios for a trace-driven LRU cache. The results indicate marked improvement in accuracy when using the proposed multifractal-based WWW model. We hope that this model can be subsequently used in cache design and evaluation studies.

### 3. Experimental data

We briefly describe the three data sets used in the modeling study. These sets were obtained from three separate WWW servers: the Computer Science Department WWW server at the University of Calgary, the WWW server at ClarkNet (a commercial Internet provider in Baltimore, Washington DC), and from the Worldcup98 WWW servers [19]. Table 1 provides a summary of the main features of the data sets. More details can be found in [2,19]. Note that the three traces have contrasting loads (in requests/second). The Calgary’s load is the lightest while the Worldcup98’s load is the heaviest.

The data sets contain several pieces of information, including the name of the host that generated the URL request, the day and time the request was recorded, the name of the requested file, the HTTP reply code (explained below), and the number of transferred bytes in response to the request. Four types of HTTP reply codes were recorded: *successful*, *not modified*, *found*, and *unsuccessful*. A *successful* code indicates that the requested file was found at the server and was returned to the client. The client may have a copy of a file, but may want to verify if this copy is up-to-date or not. If the file is up-to-date, the server

Table 1  
Summary of the data sets used in the modeling study

Feature	Trace		
	Calgary	ClarkNet	Worldcup98
Log duration	One year	One week	One day
Start date	24 Oct 1994	28 August 1995	6 May 1998
Log size (MB)	52.3	120.1	107
Total number of requests before reduction	726,739	1,164,868	1,193,353
Total number of requests after reduction	567,519	1,125,092	1,033,567
Number of unique files	8220	20,168	3824
Number of files referenced only once	1752	5279	665

responds with a *not modified* code. The *found* code indicates that the requested file is available at a different server whose address is provided in the response. Finally, the *unsuccessful* code indicates that the requested file is not available, the client has no permission to access the file, or that there is an error. In our analysis, we only included the requests with *successful* code, since they are the ones that result in actual data transfer from the server. We also excluded dynamic files (e.g., cgi and pl files).

#### 4. Multifractal analysis of WWW traffic

As indicated earlier, multifractality is a generalization of monofractality (self-similarity), where the fixed (scale independent)  $H$  parameter of a self-similar process is now scale dependent. The variability in the  $H$  value gives added flexibility to multifractal processes, allowing them to characterize irregularities in the data being modeled. Furthermore, certain multifractal processes, including the one considered in this paper, inherently exhibit an approximately lognormal-like marginal distribution, in line with the shape of the (fitting) marginal distribution of typical WWW traces. This convenient feature allows us to avoid the risky step of transforming the marginal distribution, leaving us with the task of fitting the ACF. In this section, we first briefly describe Riedi et al.’s multifractal model [17]. This model uses a wavelet-based construction to approximately capture the correlation behavior of a given time series by appropriately setting the second moments of the wavelet coefficients at each scale. Its main deficiency is its complexity, which grows linearly (in the number of parameters) with the size of the generated trace. We then describe how we modify this model to reduce its complexity to  $\mathcal{O}(1)$ , and then we apply the modified model to characterize the temporal and spatial localities of WWW traffic.

##### 4.1. Riedi et al.’s multifractal model

Riedi et al.’s model relies heavily on the discrete wavelet transform. The idea behind the wavelet transform is to express a signal (time function)

$X(t)$  by an approximated (smoothed) version and a detail. The approximation process is repeated at various levels (scales) by expressing the approximated signal at a given level  $j$  by a coarser approximation at level  $j - 1$  and a detail. At each scale, the approximation is performed through a scaling function  $\phi(t)$ , while the detail is obtained through a wavelet function  $\psi(t)$ . More formally, a wavelet expansion of the signal  $X(t)$  is given by

$$X(t) = \sum_k U_{J,k} \phi_{J,k}(t) + \sum_{j=J}^{\infty} \sum_k W_{j,k} \psi_{j,k}(t) \quad (1)$$

where

$$W_{j,k} \triangleq \int_{-\infty}^{\infty} X(t) \psi_{j,k}(t) dt, \quad (2)$$

$$U_{j,k} \triangleq \int_{-\infty}^{\infty} X(t) \phi_{j,k}(t) dt, \quad (3)$$

and  $\psi_{j,k}$  and  $\phi_{j,k}$ ,  $j, k = 0, 1, 2, \dots$ , are *shifted* and *translated* versions of the wavelet and scaling functions  $\psi(t)$  and  $\phi(t)$ , respectively, and are given by

$$\psi_{j,k}(t) \triangleq 2^{-j/2} \psi(2^{-j}t - k), \quad (4)$$

$$\phi_{j,k}(t) \triangleq 2^{-j/2} \phi(2^{-j}t - k). \quad (5)$$

In (1), the index  $J$  indicates the coarsest scale (the lowest in detail). The coefficients  $W_{j,k}$  and  $U_{j,k}$  are called, respectively, the wavelet and scale coefficients at scale  $j$  and time  $2^j k$ . Together, they define the discrete wavelet transform of the signal  $X(t)$ , assuming that  $\phi(t)$  and  $\psi(t)$  are specified. Several wavelet and scale functions have been used in the literature, giving rise to different wavelet transforms. One popular (and simple) transform is the Haar wavelet transform. This transform, which is specified by the coefficients  $W_{j,k}$  and  $U_{j,k}$  for all  $j$  and  $k$ , can be obtained recursively as follows (we adopt the same convention of [17], where the higher the value of  $j$ , the better is the approximation of the original signal):

$$U_{j,k} = \frac{U_{j+1,2k} + U_{j+1,2k+1}}{\sqrt{2}}, \quad (6)$$

$$W_{j,k} = \frac{U_{j+1,2k} - U_{j+1,2k+1}}{\sqrt{2}}. \quad (7)$$

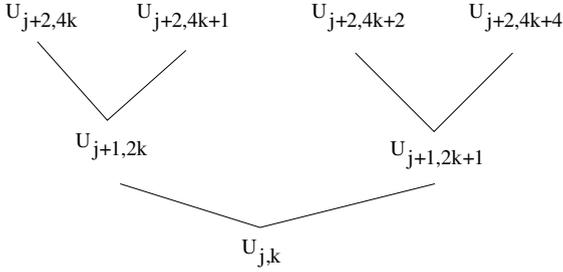


Fig. 3. Process of generating the scaling coefficients in the DWT.

To initialize the recursion, the values of  $U_{j,k}$ ,  $k = 0, 1, \dots, 2^j - 1$ , at the highest value of  $j$  are taken as the empirical trace to be modeled. Fig. 3 depicts the generation process of the scale coefficients (from top to bottom).

In order to generate synthetic traces with a given autocorrelation structure, the Haar transform is reversed by rewriting (6) and (7) as

$$U_{j+1,2k} = \frac{U_{j,k} + W_{j,k}}{\sqrt{2}}, \quad (8)$$

$$U_{j+1,2k+1} = \frac{U_{j,k} - W_{j,k}}{\sqrt{2}}. \quad (9)$$

Now to generate nonnegative data, which in our case represent the stack distance string, we need to have  $|W_{j,k}| \leq U_{j,k}$ . To satisfy this constraint, the wavelet coefficients can be defined as

$$W_{j,k} = A_{j,k} U_{j,k} \quad (10)$$

where  $A_{j,k}$  is a random variable (rv) defined on the interval  $(-1,1)$ . Using (8)–(10), the following recursion can be obtained for synthesizing the scale coefficients:

$$U_{j+1,2k} = \left( \frac{1 + A_{j,k}}{\sqrt{2}} \right) U_{j,k}, \quad (11)$$

$$U_{j+1,2k+1} = \left( \frac{1 - A_{j,k}}{\sqrt{2}} \right) U_{j,k}. \quad (12)$$

The rvs  $A_{j,k}$  must also satisfy the following additional constraints [17]:

1.  $A_{j,k}$ ,  $k = 0, 1, \dots, 2^j - 1$ , are *i.i.d* rvs that can be represented by the generic rv  $A_j$  having the same CDF as  $A_{j,k}$ .

2. For each  $j$ , the probability density function of the rvs  $A_{j,k}$ ,  $k = 0, 1, \dots, 2^j - 1$ , is symmetric with zero mean.
3.  $A_j$  is independent of  $A_l$  for  $l > j$  and is also independent of  $U_{0,0}$ .

The wavelet energy at a given scale is given by the variance of the wavelet coefficients at that scale. It has been shown that the correlation structure of the signal can be approximately captured by controlling the wavelet energy decay across scales [17]. The ratio of the energy at scale  $j - 1$  to the one at scale  $j$  ( $j$  is finer than  $j - 1$ ) was found to be [17]

$$\eta_j = \frac{E[W_{j-1}^2]}{E[W_j^2]} = 2 \frac{E[A_{j-1}^2]}{E[A_j^2](1 + E[A_{j-1}^2])}. \quad (13)$$

Assuming that  $E[W_j^2]$  is given for all  $j$ , Eq. (13) can be used to solve for  $E[A_j^2]$ ,  $j = 1, 2, \dots$ . The recursion can be initialized using  $E[A_0^2] = (E[W_0^2]/E[U_0^2])$ , where  $W_0$  and  $U_0$  are the wavelet and scale coefficients at the coarsest scale.

In [17] the authors suggested two different distributions for  $A_j$ . One of them is a symmetric beta distribution that has the following pdf:

$$f_{A_j}(x) = \frac{(1+x)^{\rho_j-1}(1-x)^{\rho_j-1}}{\beta(\rho_j, \rho_j)2^{2\rho_j-1}} \quad (14)$$

where  $\rho_j$  is the parameter of the rv and  $\beta(\cdot, \cdot)$  is the beta function. The variance of this random variable is given by

$$\text{var}[A_j] = \frac{1}{2\rho_j + 1}. \quad (15)$$

The other distribution is a point-mass distribution defined as

$$\Pr[A_j = c_j] = \Pr[A_j = -c_j] = r_j,$$

$$\Pr[A_j = 0] = 1 - 2r_j.$$

In the case of a beta distributed  $A_j$ , the parameter  $\rho_j$  at each scale can be found by solving (13) and (15), resulting in

$$\rho_j = \frac{\eta_j}{2}(\rho_{j-1} + 1) - \frac{1}{2}. \quad (16)$$

This, however, assumes that  $E[W_j^2]$  is given for  $j = 1, 2, 3, \dots$ . Since  $\eta_j$ ,  $j = 1, 2, \dots$ , cannot be

obtained using a parametric model, it must be computed from the empirical data, which makes the number of fitted parameters in the model in the order of  $N$ ;  $N$  being the trace length.

On the other hand, if  $A_j$  has a point-mass distribution, then (13) by itself is not sufficient to compute both parameters of  $A_j$  ( $c_j$  and  $r_j$ ). An alternative approach for computing these parameters is to rely on the following expression for the moments of the scaling coefficients at different scales:

$$\frac{E[U_j^q]}{E[U_{j-1}^q]} = 2^{-q/2} E[(1 + A_{j-1})^q], \quad q = 1, 2, \dots \quad (17)$$

However, to apply (17) one needs to have two moments (i.e., two values for  $q$ ) for each scale  $j$ . Again, unless we can compute these values using a parametric model, we have to rely on the empirical data to do so, which makes the model more complex than if a beta distributed  $A_j$  were to be used.

With either distribution of  $A_j$ , it was shown in [17] that the above model generates positive-valued autocorrelated data with an approximately lognormal marginal distribution.

#### 4.2. Reducing the number of parameters

As shown in the previous section, whether  $A_j$  is a beta or a point-mass rv, one needs to provide the second moments of the wavelet coefficients or two moments of the scale coefficients at each scale in order to completely determine  $A_j$ ,  $j = 1, 2, \dots$ . This significantly increases the complexity of the model, as the number of parameters to be computed a priori is in the order of the trace length. Moreover, the point-mass rv is not rich enough and takes only three possible values.

To reduce the complexity of the model, we select  $A_j$  to be a continuous-valued rv with one parameter. Then using (17) with  $q = 2$ , we compute the parameter of  $A_j$ ,  $j = 1, 2, \dots$ , with the ratio  $E[U_j^2]/E[U_{j-1}^2]$  expressed using a small number of parameters (the mean  $\mu$ , the variance  $\sigma$ , and the correlation structure of the modeled data), as shown later. The selection of the rv  $A_j$  will be discussed in Section 4.3.

For a discrete time series  $X = \{X_i: i = 1, 2, \dots, N\}$ , we define  $X^{(m)} = \{X_i^{(m)}: i = 1, 2, \dots\}$  to

be the aggregated time series of  $X$  at aggregation level  $m$ :

$$X_n^{(m)} = \sum_{i=nm-m+1}^{nm} X_i, \quad n = 1, 2, 3, \dots, N/m \quad (18)$$

where  $m = 1, 2, 4, 8, \dots, N$ . Note that if the aggregation level  $m$  corresponds to scale  $j$ , then the aggregation level  $2m$  corresponds to scale  $j - 1$ . From the definition of the Haar wavelet transform, the following holds:

$$\frac{E[(X^{(m)})^q]}{E[(X^{(2m)})^q]} = 2^{-q/2} \frac{E[U_j^q]}{E[U_{j-1}^q]}, \quad \text{for } q = 1, 2, \dots \quad (19)$$

From (19) and (17) we get

$$\frac{E[(X^{(m)})^q]}{E[(X^{(2m)})^q]} = 2^{-q} E[(1 + A^{(2m)})^q] \quad (20)$$

where  $A^{(2m)} = A_{j-1}$ . Evaluating (20) at  $q = 2$ , we obtain the following expression:

$$E[(A^{(2m)})^2] = 4 \frac{E[(X^{(m)})^2]}{E[(X^{(2m)})^2]} - 1. \quad (21)$$

To reduce the number of parameters in the multifractal model, we need to analytically obtain  $E[(X^{(m)})^2]$  for all possible values of  $m$ . The variance at aggregation level  $m$ ,  $\text{var}[X^{(m)}] \triangleq V^{(m)}$ , can be expressed in terms of the autocorrelation function of the signal [6]:

$$V^{(m)} = mv + 2v \sum_{k=1}^m (m-k) \rho_k. \quad (22)$$

The mean,  $E[(X^{(m)})] = \mu^{(m)}$ , is given by

$$\mu^{(m)} = m\mu \quad (23)$$

where  $\mu$  and  $v$  are the mean and variance of the original signal, respectively. The second moment of  $X^{(m)}$  is then given by

$$E[(X^{(m)})^2] = mv + 2v \sum_{k=1}^m (m-k) \rho_k + m^2 \mu^2. \quad (24)$$

From (21) and (24), the parameter of the rv  $A_j$  can be computed for all scales  $j = 1, 2, \dots$ , given  $\mu$ ,  $v$ , and the correlation structure of the time series being modeled. For normalized stack distance

strings, we found that the form  $\rho_k = e^{-\beta\sqrt{g(k)}}$ ,  $k = 0, 1, \dots$ , fits the correlation structure very well, where  $g$  is a function of the lag  $k$ . For both the ClarkNet and the Worldcup98 traces,  $g(k) = k$  produced a good fit to the empirical ACF, while for the Calgary trace,  $g(k) = \log(k + 1)$  was found appropriate. Fig. 4 shows the fitting of the ACF functions for the three traces.

In summary, to use the multifractal model for modeling the normalized stack distance string, we only need five parameters:

- Mean of the normalized stack distance string ( $\mu$ ).
- Variance of the normalized stack distance string ( $v$ ).
- Autocorrelation structure (parameterized by  $\beta$ ,  $n$ , and  $g$ ).

Using these parameters, along with (24) and (21), one can compute the parameter of the rv  $A_j$  at each aggregation level (scale).

The synthesis process starts from the highest level of aggregation. At this level we can start with  $l$  data points that are normally distributed with mean  $m_h\mu$  (the mean at aggregation level  $m_h$ ) and variance of  $\text{var}[X^{(m_h)}]$ , where  $m_h$  is the highest aggregation level. After that, the process can be carried out using (11) and (12).

### 4.3. Selecting the random variable $A_j$

As indicated earlier, the rv variable  $A_j$  must be symmetric with zero mean and defined on the in-

terval  $(-1,1)$ . To reduce the number of parameters of the multifractal model, we require that  $A_j$  is specified by one parameter only. There are many rvs that can satisfy these conditions. The difference between one rv and another is the range of the values that the ratio  $E[(X^{(m)})^2]/E[(X^{(2m)})^2]$  can take. It can be shown that for any distribution, this ratio satisfies the following inequalities:

$$0.25 \leq \frac{E[(X^{(m)})^2]}{E[(X^{(2m)})^2]} \leq 0.5. \tag{25}$$

The lower bound follows immediately from (21) and the fact that  $E[(A^{(2m)})^2] \geq 0$ . The proof for the upper bound is provided in the appendix. As an example, consider the uniform rv in the range  $[-c, c]$ , where  $|c| < 1$ . The variance of this rv is given by  $V = c^2/3$ . Solving (21) for  $c$ , we get

$$c = 3 \left( 4 \frac{E[(X^{(m)})^2]}{E[(X^{(2m)})^2]} - 1 \right).$$

Since  $c < 1$ ,

$$\frac{E[(X^{(m)})^2]}{E[(X^{(2m)})^2]} < \frac{1}{3}.$$

Using similar calculations, Table 2 shows the upper bound for a number of popular rvs.

For the three traces we use in this work, the ratio  $E[(X^{(m)})^2]/E[(X^{(2m)})^2]$  studied never exceeded 0.3333, and as a result, we decided to use the uniform rv since it is the simplest one.

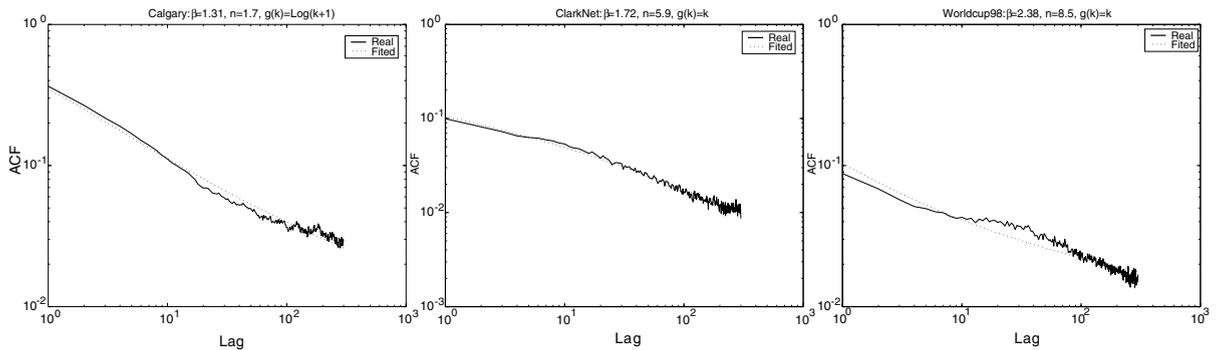


Fig. 4. Fitting the correlation structure of the normalized stack distance string.

Table 2  
Upper bound on the ratio  $E[(X^{(m)})^2]/E[(X^{(2m)})^2]$  for various distributions

Random variable	Upper bound
Symmetric beta ( $\rho, \rho$ )	0.5000
Uniform ( $-c, c$ )	0.3333
Triangular ( $-c, 0, c$ )	0.2917
Normal ( $0, \sigma$ )	0.2778

## 5. Modeling WWW traffic

In this section, we describe our approach for modeling the stream of file objects generated by a WWW server. Let  $U$  be the number of unique files (or objects) at the server and let  $fr_i$  be the fraction of requests for the  $i$ th file,  $i = 1, 2, \dots, U$  (i.e., the popularity index of file  $i$ ). The modeling approach proceeds in three steps. First, we extract the stack distance string from the URL reference string. Then, we apply some form of normalization to capture both sources of temporal locality (temporal correlation and long-term popularity). The modified multifractal model described in the previous section is then applied to model the normalized stack distance string. Finally, we incorporate the popularity profile of the traffic during the process of generating synthetic reference strings. These steps are described next.

### 5.1. Extracting the empirical normalized stack distance string

In our model, we use the concept of stack distance to model the temporal and spatial localities in WWW traffic. The authors in [3] extract the stack distances from the original trace assuming an arbitrary initial ordering of the stack. Whenever an object is requested, its depth in the stack (stack distance) is recorded and the object is pushed to the top of the stack. In our model, we avoid making any assumptions on the initial ordering of the stack, which we have found to disturb the marginal distribution and the correlation structure of the stack distance string. We start with an empty stack and process the empirical reference string *in the reverse direction*, starting from the last reference. If a file is referenced for the first time (in the reverse direction), it is put on top of the stack

but no stack distance is recorded. Otherwise, if the file has already been referenced before (hence, it is already in the stack), then it is pushed from its previous location in the stack to the top of the stack and its depth is recorded as a stack distance. Finally, the resulting trace of stack distances is reversed to get the correct stack distance string. The following example illustrates the idea. Consider the reference string [a d c b c d d a b], where each letter indicates the name of a file. If we process this string starting from the end, the first reference is to file b. Since this is the first time file b is being referenced, we push it to the top of the stack without recording any distance. The same procedure is performed for the next two references (for files a and d). The fourth reference (from the end) is for file d. Since this file has been referenced before, it gets pushed to the top of the stack and its stack depth is recorded (in this case, the stack depth for file d is one). The procedure continues until all references are processed (see Fig. 5). The end result of this process is the stack distance stream [4 3 2 4 1].

Temporal locality in a stream of WWW requests is attributed to two factors: long-term popularity and short-term temporal correlations. Both factors are important for cache design [14,15], and must therefore be incorporated in the model for temporal locality. In [15], it was found that the (lognormal) distribution of the stack distance string is predominantly affected by the popularity profile (i.e., long-term popularity). So the marginal distribution of the stack distance (without normalization) does not capture the effect of short-term temporal correlations.

To accurately capture the temporal locality of the traffic, we need to isolate the effect of popularity from that of short-term correlations. One solution is to have a separate stack-distance-string model for equally popular objects. Another solution, used in our work, is to capture how much a stack distance deviates from its “expected” value. This deviation is captured by normalizing (scaling) the stack distances by their expected values. The resulting scaled stack distance string is a measure of how objects are clustered over the trace length (temporal correlation). This measure is insensitive to the popularity profile, so it allows us to

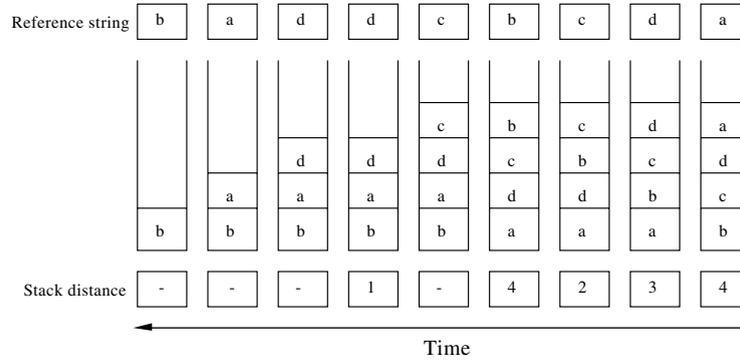


Fig. 5. Example showing our approach for extracting stack distances from a real trace.

separately model the popularity profile and the short-term temporal correlations.

The expected stack distance for a file  $i$  is computed as follows:

$$E[d_i] = \sum_{g \neq i} \frac{f_g}{f_g + f_i - 1} \quad (26)$$

where  $f_i$  is the number of references to file  $i$  [5]. For the three studied traces, we found that the normalized stack distance string has an approximately lognormal marginal distribution. Fig. 6 shows the fitting of the lognormal marginal distribution of the normalized stack distance string.

### 5.2. Modeling the normalized stack distance string

To model the normalized stack distance string, we need to determine  $\mu$ ,  $v$ ,  $\beta$ , and  $n$ . Once the values of these parameters are determined, the

multifractal model described in Section 4 can be used to capture the marginal distribution and the correlation structure of the normalized stack distance string. Note that spatial locality is captured by modeling the autocorrelation function of the *unscaled* stack-distance string. However, since the multifractal model is applied to the scaled version of the stack-distance string, we have to invert back the synthesized trace of the multifractal model so that the resulting trace models the unscaled version of the data. The pseudo-code in Fig. 7 describes the modeling process. The function GenNormStackDistance takes five input parameters. The first three parameters are  $\mu$ ,  $v$ , and the ACF of the normalized stack distance string to be generated. The fourth parameter,  $N$ , is the length of the synthetic normalized stack distance string. The fifth parameter,  $l$ , is the number of data points at the coarsest scale. GenNormStackDistance

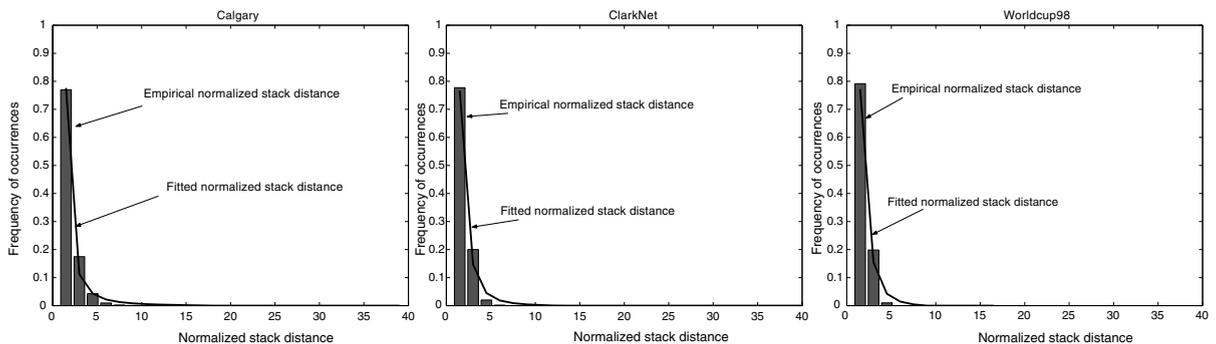


Fig. 6. Marginal distribution of the normalized stack distance string.

```

GenNormStackDistance( $\mu, v, \rho_k, N, l$ )
2   $NumAggLevels = \lceil \log_2(N/l) \rceil$ 
3   $m = 1$ 
4   $SecMom(1) = mv + m^2\mu^2$ 
5  for  $i = 2$  to  $NumAggLevels$  Do
6     $m = 2m$ 
7     $sum = 0$ 
8    for  $k = 1$  to  $m$  Do
9       $sum = sum + (m - k)\rho_k$ 
10   end for
11    $SecMom(i) = mv + 2v sum + m^2\mu^2$ 
12    $SecMom\_ratios(NumAggLevels - i + 1) = \frac{SecMom(i-1)}{SecMom(i)}$ 
13    $AParm(NumAggLevels - i + 1) = \sqrt{3(4 SecMom\_ratio(NumAggLevels - i + 1) - 1)}$ 
14 end for
15  $\mu_h = 2^{(NumAggLevels-1)} * \mu$ 
16  $V_h = SecMom(NumAggLevels) - \mu_h^2$ 
17  $NormStkDist = norm\_random(\mu_h, \sqrt{V_h}, l)$ 
18  $i = 1$ 
19 While( $length(NormStkDist) < N$ ) Do
20    $A = Uniform\_random(-AParm(i), AParm(i), length(NormStkDist))$ 
21    $NormStkDist = \lfloor NormStkDist \frac{(1+A)}{2} \rfloor \lfloor NormStkDist \frac{(1-A)}{2} \rfloor$ 
22    $i = i + 1$ 
23 end while
END

```

Fig. 7. Algorithm for generating synthetic scaled stack distance strings.

starts by computing the number of aggregation levels,  $NumAggLevels$  (line 2). In line 4, the second moment of the normalized stack distance string at aggregation level  $m = 1$  is computed. The for loop starting in line 5 is used to compute the second moment for the remaining aggregation levels. The for loop that starts from line 8 computes the summation in (24). In line 11, the second moments at higher aggregation levels are computed using (24). The second moments ratio,  $E[(X^{(m)})^2]/E[(X^{(2m)})^2]$ , is computed in line 12. The parameter of the rv  $A^{(2m)}$  is computed in line 13 using (21) and substituting for the variance of the uniform rv in  $E[(X^{(2m)})^2]$ . After computing these parameters, the mean of the time series at the highest aggregation level is computed in line 15 using (23). The variance at the highest aggregation level is computed in line 16. In line 17,  $l$  data points are generated to represent the coarsest level. The while loop starting from line 19 is used to continue the generation process using (11) and (12).

### 5.3. Modeling popularity and generating synthetic reference strings

To generate a synthetic WWW reference string, we first generate a synthetic normalized stack distance string, as shown in the previous section. The process of generating a synthetic WWW reference

string starts by arranging the unique documents of the WWW server in an LRU stack. This is done by sampling from a probability distribution that is weighted by the popularity profiles of the various documents (i.e., the more popular a document is, the more likely it will be placed closer to the top of the stack). This ordering approach was used in [5]. It is known to provide more accurate results than using an arbitrary ordering. Note that even though the probability of selecting a *given* unpopular document is small, the probability of selecting *any* of the unpopular documents is relatively large (because of the large number of unpopular documents). So, probabilistically, there is a good chance that *some* unpopular documents will be placed near the top of the stack. To generate a reference string of length  $N$ , we first compute the number of references a document can get according to its popularity profile. Then, the top document in the LRU stack is considered as the next referenced document in the synthetic reference string. If the required number of references for this document is reached, then this document is flushed out of the stack. Otherwise, it is pushed down the stack according to the next value in the stack distance string (obtained after scaling back the normalized stack distance by multiplying it by the corresponding expected stack distance for the object in hand). Note that our notion of a “stack” allows for the insertion of an object in between two

```

GenTrace(NormStkDist, req, lru)
2  i = 0
3  k = 0
4  While(stack is not empty) Do
5    Ref(i) = top(lru)
6    i = i + 1
7    req(Ref(i)) = req(Ref(i)) - 1
8    if (req(Ref(i)) == 0) then
9      drop document from the stack
10   else
11     StkDist = Scale-Back(NormStkDist(k), Ref(i))
12     Push-Top-Documen-Down-Stack(StkDist)
13     k = k + 1
14   endif
15 end while
END

```

Fig. 8. Algorithm for generating synthetic WWW strings.

objects in the stack, which does not happen in a regular LRU stack. This process continues until the popularity profiles of all objects are satisfied (no documents are left in the LRU stack). The pseudo-code in Fig. 8 describes the generation process. Function *GenTrace* accepts three parameters: the synthetic normalized stack distance (*NormStkDist*), the number of requests each file gets (*req*), and the *lru* stack with the files ordered according to the popularity profile (placed randomly according to the empirical distribution of the popularity profiles). The while loop in line 4 is used to generate the reference string. Line 5 is used to record the next reference, *Ref*(*i*), taken as the file at the top of the LRU stack. Then the number of outstanding references to this file, *req*(*Ref*(*i*)), is reduced by one (line 7). If this number reaches

zero, then the file is dropped out the stack. Otherwise, the next stack distance, *StkDist*, is computed in line 11 by scaling back the normalized stack distance according to the popularity of the file. The file is then pushed *StkDist* positions down the stack. The while loop in line 4 is continued until the LRU stack is empty.

## 6. Experimental results

In this section, we evaluate the accuracy of the proposed multifractal model and contrast it with two other models. The first model is a self-similar (monofractal) model [1,3]. This model involves transforming the Gaussian marginal distribution of a fractional ARIMA process into a lognormal distribution. We simply refer to this model as the LRD model. The second model was proposed by Cherkasova et al. [5]. The three investigated models were mainly designed for offline traffic generation, with the primary purpose of generating synthetic traces for use in cache design studies. Accordingly, we compare these models in terms of the file and byte miss ratios seen at an LRU cache that is driven by synthetic traces from these models. The comparison is made with reference to the cache performance seen under the real traffic. The results are shown in Figs. 9–11.

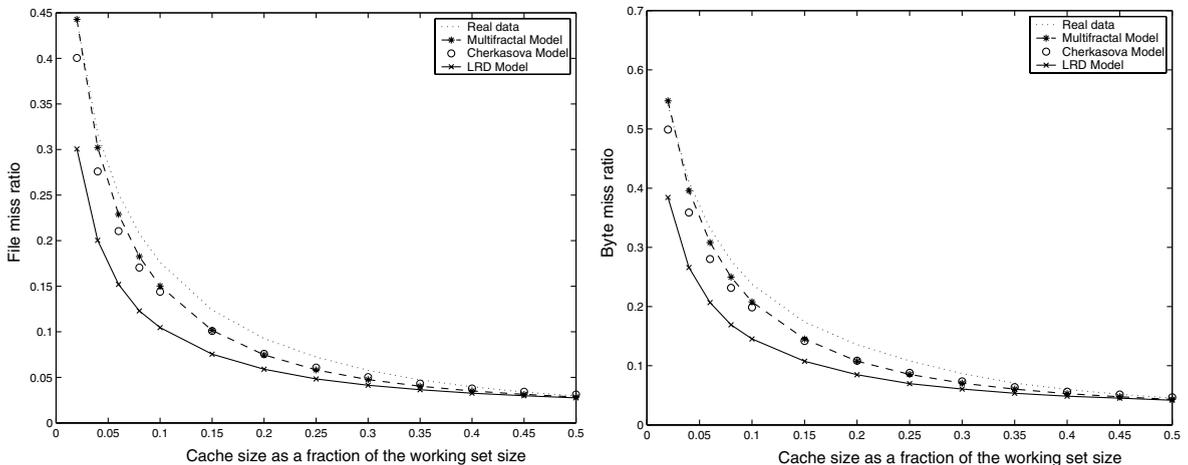


Fig. 9. File and byte miss ratios versus cache size (Clarknet trace).

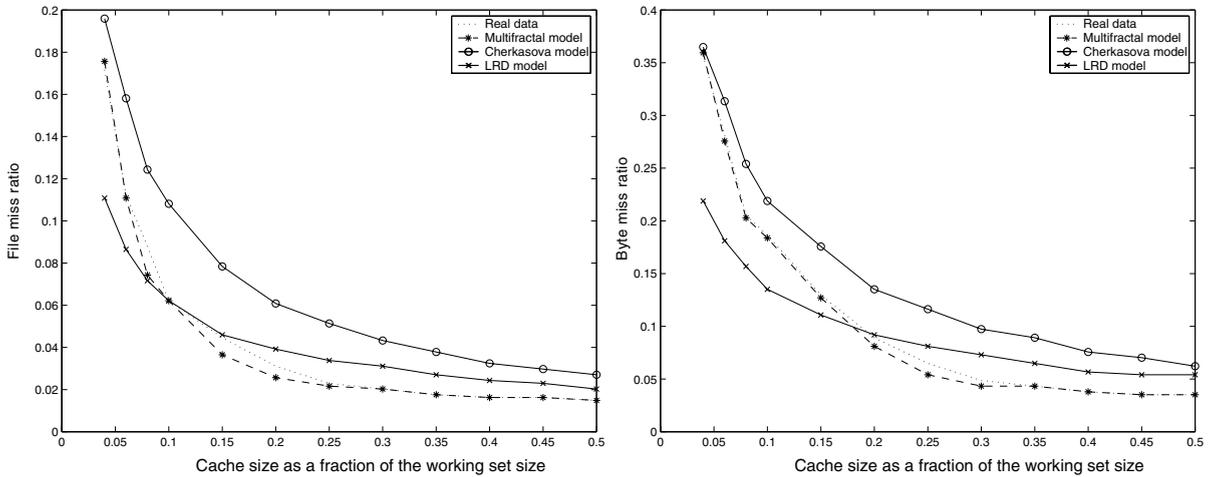


Fig. 10. File and byte miss ratios versus cache size (Calgary trace).

It is clear that of the three models, the proposed multifractal model produces the most accurate results, especially for small cache sizes. The relative accuracy in terms of capturing the behavior of the real data is greater in the case of the Calgary data. Consider, for example, the Calgary data with a normalized cache size of 0.3. The percentage inaccuracies in the file miss rate for the multifractal model, the LRD model, and Cherkasova et al.’s model are 0.5%, 53%, and 111%, respectively. In the case of the byte miss rate, the corresponding values are 4.9%, 65%, and 109%.

The overall improvement in the accuracy of the file and byte miss rates due to the use of the multifractal model is significant. Moreover, our model captures the spatial locality which is not reflected through the file/byte miss ratios of the LRU caching policy. To show how well our model captures this property, we also compared the inter-request “times” (number of requested files between any two references to a given file) in the real data to those in the synthetic traces of the models. We found that the sequence of inter-request times is nonstationary (has a clear decreasing trend). So we

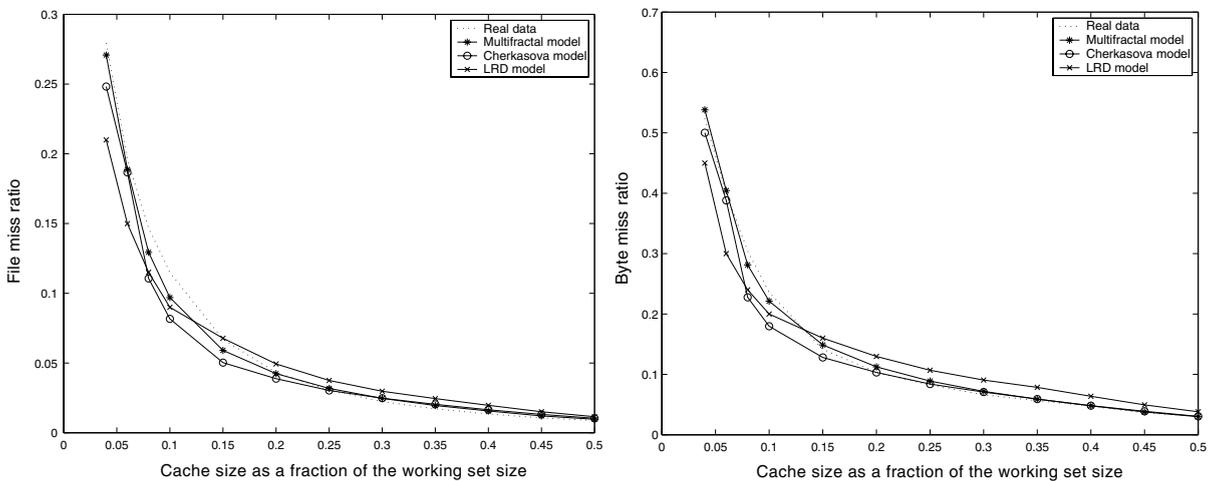


Fig. 11. File and byte miss ratios versus cache size (Worldcup98 trace).

Table 3  
Statistical comparisons for CLARKNET trace

Statistic		Real data	Multifractal model	Cherkasova's model	LRD model
$\mu$		0.954	0.937	0.806	0.905
$\sigma$		1.032	1.164	1.918	1.428
$\rho_1$		0.130	0.118	0.000	0.060
$\rho_5$		0.076	0.075	0.000	0.020
$\rho_{10}$		0.061	0.058	0.000	0.009
$\rho_{25}$		0.039	0.039	0.000	0.001
Percentiles	75%	1.306	1.149	0.778	1.063
	90%	2.233	2.210	1.697	2.161
	98%	3.976	4.230	4.980	5.051

Table 4  
Statistical comparisons for CALGARY trace

Statistic		Real data	Multifractal model	Cherkasova's model	LRD model
$\mu$		0.714	0.68	0.62	0.907
$\sigma$		1.541	2.010	7.080	4.224
$\rho_1$		0.192	0.185	0.000	0.030
$\rho_5$		0.070	0.063	0.000	0.030
$\rho_{10}$		0.036	0.036	0.000	0.027
$\rho_{25}$		0.009	0.010	0.000	0.023
Percentiles	75%	0.813	0.813	0.771	0.326
	90%	1.790	1.790	2.293	2.046
	98%	4.289	5.241	5.531	6.644

Table 5  
Statistical comparisons for WORLDCUP98 trace

Statistic		Real data	Multifractal model	Cherkasova's model	LRD model
$\mu$		0.990	0.951	0.823	0.941
$\sigma$		0.986	1.137	1.718	1.289
$\rho_1$		0.054	0.054	0.000	0.098
$\rho_5$		0.027	0.037	0.000	0.089
$\rho_{10}$		0.025	0.030	0.000	0.071
$\rho_{25}$		0.022	0.023	0.000	0.034
Percentiles	75%	1.373	1.136	0.856	1.134
	90%	2.266	2.099	1.727	2.101
	98%	3.843	4.210	4.666	4.726

normalized this sequence by the *expected* inter-request time, which is equal to  $1/fr_i$  for file  $i$ . The mean, variance, percentile values, and some values of the autocorrelation function for the normalized inter-request times are shown in Tables 3–5. Note that the mean, variance, percentile values of the inter-request times are measures of the temporal locality, while the autocorrelation is a measure of the spatial locality.

From these results, it is clear that the multifractal model is more accurate than the other two models in capturing these statistics.

## 7. Conclusions

In this work, we demonstrated the potential of multifractal processes as a viable approach for WWW traffic modeling. We started with the mul-

tifractal model of Riedi et al., which is capable of generating approximately lognormal synthetic traces with any desired autocorrelation structure. However, to apply this model in traffic fitting and trace generation, one needs to match as many parameters of the model as the length of the trace to be generated. To make the model parsimonious, we modified it by using a different distribution for the multiplier  $A_j$  (which relates the wavelet and scale coefficients) and by analytically expressing the parameter of  $A_j$ ,  $j = 1, 2, \dots$ , in terms of the mean, variance, and ACF of the modeled data. As a result, the modified multifractal model is specified by five parameters only. We fitted this model to the normalized stack distance strings of three WWW traffic traces. The proposed model captures the spatial and temporal localities of the real traffic as well as the popularity profile. Trace-driven simulations of the LRU cache policy indicates that the proposed model gives much more accurate cache miss rates than two previously proposed WWW traffic models. Statistics of the normalized inter-request distances support the goodness of our model. Our future research will focus on designing new cache replacement and prefetching policies that exploit the characteristics of the traffic and that rely on model predictions in making file replacement and prefetching decisions.

### Acknowledgements

This work was supported by the National Science Foundation under grants ANI 9733143, CCR 9979310, and ANI 0095626; by a scholarship from the government of Saudi Arabia through King Abdul-aziz University; by a grant from the University of Arizona (Proposition 301 initiative); and by the Center for Low Power Electronics (CLPE) at the University of Arizona (Grant EEC-9523338). An abridged version of this paper was presented at the Web Engineering Workshop, Pisa, Italy, May 2002.

### Appendix A

Let  $X \triangleq \{X_i; i = 1, 2, \dots\}$  be a positive valued stationary random process, and let  $Y \triangleq \{Y_i; i =$

$1, 2, \dots\}$  be an aggregation of  $X$  that is defined as follows:

$$Y_n = X_{2n-1} + X_{2n}.$$

Note that  $X^{(m)}$  in (25) represents  $X$ , while  $X^{(2m)}$  represents  $Y$ . We now prove that  $E[X_n^2]/E[Y_n^2] \leq 0.5$ .

$$\begin{aligned} \frac{E[X_n^2]}{E[Y_n^2]} &= \frac{E[X_n^2]}{E[(X_{2n-1} + X_{2n})^2]} \\ &= \frac{E[X_n^2]}{E[X_{2n-1}^2 + 2X_{2n-1}X_{2n} + X_{2n}^2]} \\ &= \frac{E[X_n^2]}{E[X_{2n-1}^2] + 2E[X_{2n-1}X_{2n}] + E[X_{2n}^2]}. \end{aligned}$$

Since  $X$  is stationary,  $E[X_{2n-1}^2] = E[X_{2n}^2] = E[X_n^2]$ , which leads to

$$\begin{aligned} \frac{E[X_n^2]}{E[Y_n^2]} &= \frac{E[X_n^2]}{2E[X_n^2] + 2E[X_{2n-1}X_{2n}]} \\ &= \frac{1}{2 + 2E[X_{2n-1}X_{2n}]/E[X_n^2]} \leq 0.5 \end{aligned}$$

since  $E[X_{2n-1}X_{2n}]/E[X_n^2] \geq 0$ .

### References

- [1] V. Almeida, A. Bestavros, M. Crovella, A. Oliverira, Characterizing reference locality in the WWW, in: Proceedings of the Fourth International Conference on Parallel and Distributed Information Systems (PDIS), 1996, pp. 92–103.
- [2] M. Arlitt, C. Williamson, Web server workload characterization: the search for invariants, in: Proceedings of the ACM SIGMETRICS Conference, 1996, pp. 126–137.
- [3] P. Barford, M. Crovella, Generating representative Web workloads for network and server performance evaluation, in: Proceedings of the ACM SIGMETRICS Conference, 1998, pp. 151–160.
- [4] P. Cao, S. Irani, Cost-aware WWW proxy caching algorithms, in: Proceedings of the 1997 USENIX Symposium on Internet Technology and System, 1997, pp. 193–206.
- [5] L. Cherkasova, G. Ciardo, Characterizing temporal locality and its impact on Web server performance, in: Proceedings of the Ninth International Conference on Computer Communication and Networks (ICCCN), 2000, pp. 434–441.
- [6] D. Cox, Long-range dependence: a review. Statistics: an appraisal, The Iowa State University, Ames, Iowa, 1984, pp. 55–74.

- [7] C. Cunha, A. Bestavros, M. Crovella, Characteristics of WWW client-based traces, *IEEE/ACM Transactions on Networking* 1 (3) (1999) 134–233.
- [8] A. Feldman, A. Gilbert, W. Willinger, T. Kurtz, The changing nature of network traffic: scaling phenomena, in: *Proceedings of the ACM SIGCOMM Conference*, vol. 2, 1998, pp. 5–29.
- [9] J. Gao, I. Rubin, Multifractal analysis and modeling of long-range dependent traffic, in: *Proceedings of the IEEE International Conference on Communications (ICC)*, vol. 1, 1999, pp. 382–386.
- [10] A. Gilbert, W. Willinger, A. Feldmann, Scaling analysis of conservative cascades, with applications to network traffic, *IEEE Transactions on Information Theory—Special Issue on Multiscale Statistical Signal Analysis and its Applications* 45 (3) (1999) 971–991.
- [11] A. Gillbert, W. Willinger, Scaling analysis of conservative cascades with applications to network traffic, in: *Proceedings of the ACM SIGCOMM Conference*, vol. 4, 1998, pp. 42–55.
- [12] C. Huang, M. Devetsikiotis, I. Lambadaris, A.R. Kays, Modeling and simulation of self-similar variable bit rate compressed video: a unified approach, in: *Proceedings of the ACM SIGCOMM Conference*, vol. 25, 1995, pp. 114–125.
- [13] S. Jin, A. Bestavros, Popularity-aware greedy-dual size web proxy caching algorithms, in: *Proceedings of the International Conference on Distributed Computing Systems (ICDCS)*, Taiwan, 2000.
- [14] S. Jin, A. Bestavros, Sources and characteristics of web temporal locality, in: *Proceedings of IEEE/ACM International Symposium on Modeling, Analysis and Simulation of Computer and Telecommunication Systems*, San Francisco, CA, 2000.
- [15] S. Jin, A. Bestavros, Temporal locality in web request streams, in: *Proceedings of the ACM SIGMETRICS Conference*, 2000, pp. 110–111.
- [16] S. Jin, A. Bestavros, Greedy-dual\* Web caching algorithm, *International Journal on Computer Communications* 24 (2) (2001) 174–183.
- [17] R. Riedi, M. Crouse, V. Ribeiro, R. Baraniuk, A multifractal wavelet model with application to network traffic, *IEEE Transactions on Information Theory* 45 (3) (1999) 992–1018.
- [18] R. Riedi. Introduction to multifractals, <http://www.dsp.rice.edu/publications/>.
- [19] Internet traffic archive at <http://ita.ee.lbl.gov/>.

**Abdullah Balamash** received the B.S. degree in Electrical and Computer Engineering from King Abdul-aziz University, Jeddah, Saudi Arabia, in 1991. From 1991 to 1994, he worked for the Saudi Consolidated Electricity company as a system engineer. In January 1995, he joined the Department of Electrical and Computer Engineering of King Abdul-aziz University as a teaching assistant.

In August 1996, he got a scholarship from the Saudi government to pursue his M.S. and Ph.D. degrees. He received his M.S. degree in Electrical and Computer Engineering from Syracuse University, New York, in 1999. He is currently working toward his Ph.D. degree at the University of Arizona. His research interests are in traffic analysis, network systems modeling, and performance evaluation.

**Marwan Krunz** received his Ph.D. degree in Electrical Engineering from Michigan State University, Michigan, in 1995. From 1995 to 1997, he was a Postdoctoral Research Associate with the Department of Computer Science and the Institute for Advanced Computer Studies (UMIACS), University of Maryland, College Park. In January 1997, he joined the University of Arizona, where he is currently an Associate Professor of Electrical and Computer Engineering. His research interests lie in the field of computer networks, especially in its performance and traffic control aspects. His recent work has focused on the provisioning of quality of service (QoS) over wireless links, QoS routing (path selection, state aggregation), traffic modeling (video, WWW), bandwidth allocation, video-on-demand systems, and power-aware protocols for ad hoc networks. He has published more than 60 journal articles and refereed conference papers.

He is a recipient of the National Science Foundation CAREER Award (1998–2002). He currently serves on the editorial board for the *IEEE/ACM Transactions on Networking*, the *Computer Communications Journal*, and the *IEEE Communications Interactive Magazine*. He is a guest co-editor of a special issue on Hot Interconnects (*IEEE Micro*, January 2002) and of a Feature Topic on QoS Routing (*IEEE Communications*, June 2002). He is the Technical Program Co-chair for the IEEE INFOCOM 2004 Conference. He was the Technical Program Co-chair for the 9th Hot Interconnects Symposium (Stanford University, August 2001). He has served and continue to serve on the executive and technical program committees of many international conferences. He served as a reviewer and a panelist for NSF proposals, and is a consultant for several corporations in the telecommunications industry.