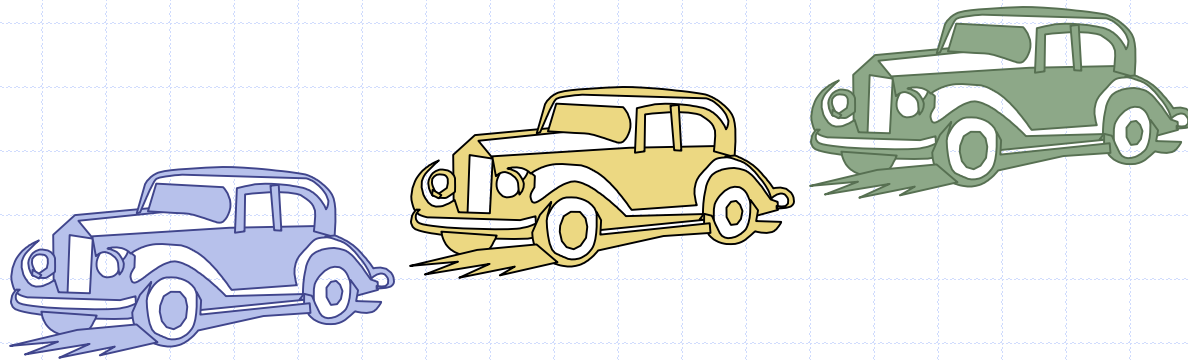


Queues



Outline and Reading

- ◆ The Queue ADT (§2.1.2)
- ◆ Implementation with a circular array (§2.1.2)
- ◆ Growable array-based queue
- ◆ Queue interface in Java

The Queue ADT

- ◆ The **Queue** ADT stores arbitrary objects
- ◆ Insertions and deletions follow the first-in first-out scheme
- ◆ Insertions are at the rear of the queue and removals are at the front of the queue
- ◆ Main queue operations:
 - **enqueue**(object): inserts an element at the end of the queue
 - object **dequeue**(): removes and returns the element at the front of the queue
- ◆ Auxiliary queue operations:
 - object **front**(): returns the element at the front without removing it
 - integer **size**(): returns the number of elements stored
 - boolean **isEmpty**(): indicates whether no elements are stored
- ◆ Exceptions
 - Attempting the execution of dequeue or front on an empty queue throws an **EmptyQueueException**

Applications of Queues

◆ Direct applications

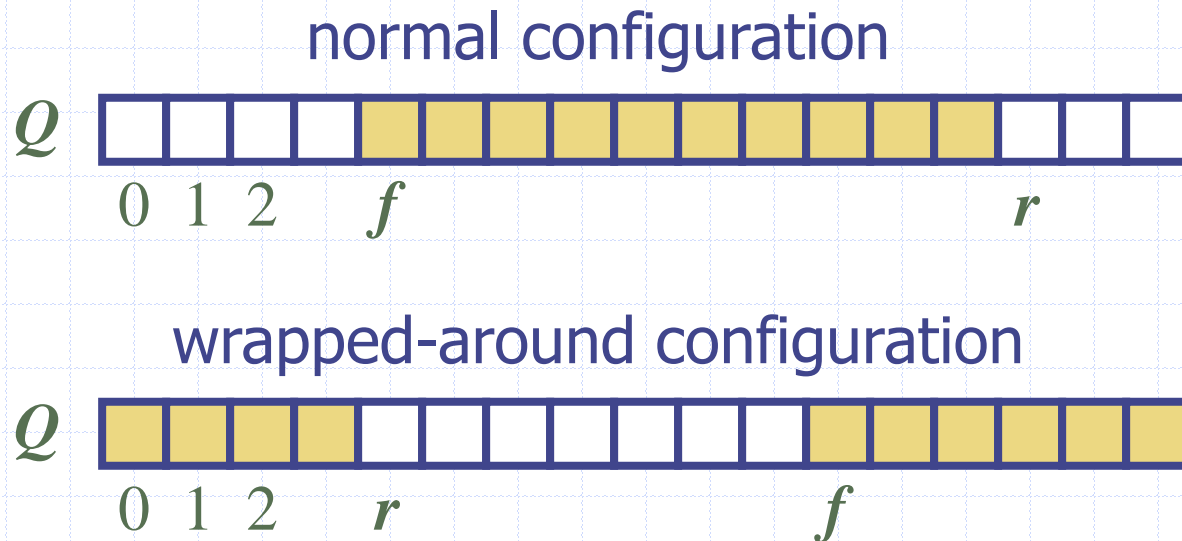
- Waiting lists, bureaucracy
- Access to shared resources (e.g., printer)
- Multiprogramming

◆ Indirect applications

- Auxiliary data structure for algorithms
- Component of other data structures

Array-based Queue

- ◆ Use an array of size N in a circular fashion
- ◆ Two variables keep track of the front and rear
 - f index of the front element
 - r index immediately past the rear element
- ◆ Array location r is kept empty



Queue Operations

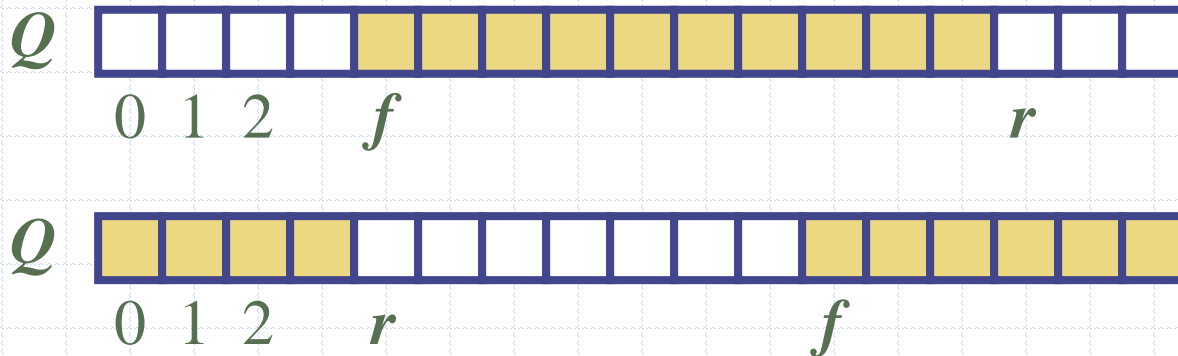
- ◆ We use the modulo operator (remainder of division)

Algorithm *size()*

return $(N - f + r) \bmod N$

Algorithm *isEmpty()*

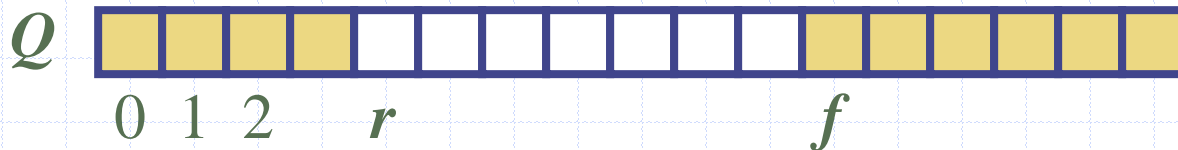
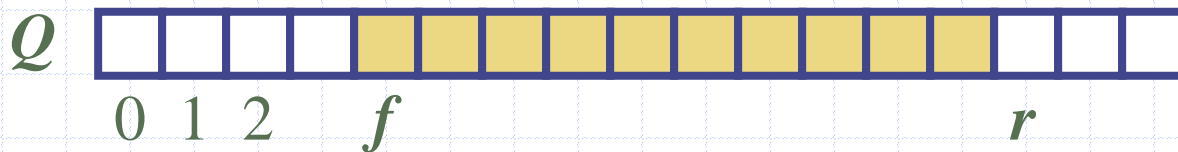
return $(f = r)$



Queue Operations (cont.)

- ◆ Operation enqueue throws an exception if the array is full
- ◆ This exception is implementation-dependent

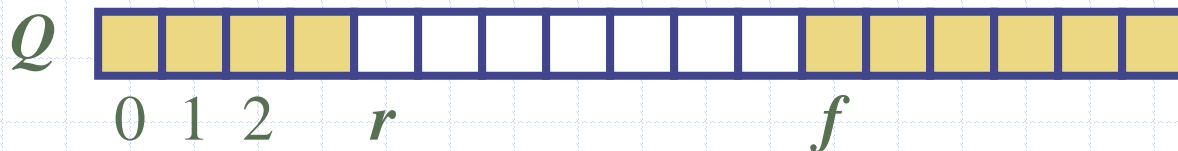
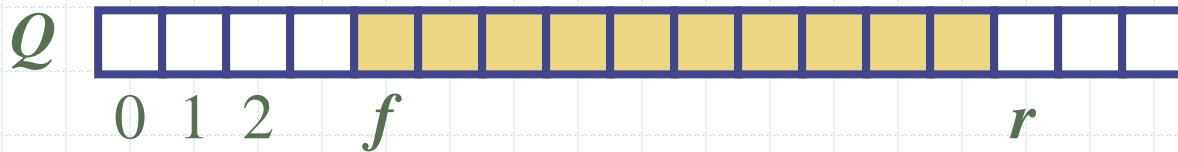
```
Algorithm enqueue(o)  
  if  $size() = N - 1$  then  
    throw FullQueueException  
  else  
     $Q[r] \leftarrow o$   
     $r \leftarrow (r + 1) \bmod N$ 
```



Queue Operations (cont.)

- ◆ Operation `dequeue` throws an exception if the queue is empty
- ◆ This exception is specified in the queue ADT

```
Algorithm dequeue()  
if isEmpty() then  
    throw EmptyQueueException  
else  
     $o \leftarrow Q[f]$   
     $f \leftarrow (f + 1) \bmod N$   
    return  $o$ 
```



Growable Array-based Queue

- ◆ In an enqueue operation, when the array is full, instead of throwing an exception, we can replace the array with a larger one
- ◆ Similar to what we did for an array-based stack
- ◆ The enqueue operation has amortized running time
 - $O(n)$ with the incremental strategy
 - $O(1)$ with the doubling strategy

Queue Interface in Java

- ◆ Java interface corresponding to our Queue ADT
- ◆ Requires the definition of class `EmptyQueueException`
- ◆ No corresponding built-in Java class

```
public interface Queue {  
    public int size();  
    public boolean isEmpty();  
    public Object front()  
        throws EmptyQueueException;  
    public void enqueue(Object o);  
    public Object dequeue()  
        throws EmptyQueueException;  
}
```