# Storage Problem 

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## Plan for the talk:

- Storage problem
- Real world problem
- Graph construction
- Special properties
- Problem solution


## Storage Problem

A company manufactures chemicals. On demand the company supplies chemicals to customers. The company produces $n$ number of chemicals, in which some of them are not compatible with few others. While storing the chemicals altogether in a warehouse might result in explosion. In order to avoid collision the warehouse is to be partitioned into different compartments for the storage of compatible chemicals into one compartment.

## Real world problem

- Below is the matrix representation of compatibility relationship between different chemical products stored, it explains whether the chemical can be stored along with that particular chemical product or not.


## Compatibility check Matrix

|  | Inorganic acids | $\begin{aligned} & \text { y } \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | 8 0 0 0 0 | 髟 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Inorganic acids |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| Organic acids | $\checkmark$ |  |  | $\checkmark$ |  |  |
| Caustics | $\checkmark$ |  |  |  |  | $\checkmark$ |
| Amines | $\checkmark$ | $\checkmark$ |  |  | $\checkmark$ |  |
| Halogenated compounds |  |  |  | $\checkmark$ |  |  |
| Alcohols, Glycol, Glycol Ether | $\checkmark$ |  | $\checkmark$ |  |  |  |

## Graph construction

From the adjacency matrix we represent the problem in the graph format.

- Consider each chemical as a vertex.
- Join two vertices if and only if they are not compatible with each other.
- Complete the construction of graph by considering the adjacency list.


## Adjacency List

| vertices | incompatible <br> vertex |
| :---: | :--- |
| a | b c d f |
| b | a d |
| c | a d f |
| $d$ | a b c e |
| e | d |
| f | a c |

## Interpreting graph for real world problem



## Interval graph

## B



## Special properties

- Vertex coloring: Assigning of colors to labels of a graph G such that no two vertices of a edge have identical colors.
- Chromatic number: Chromatic number G of a graph is the minimum number of colors require to color the vertices of a graph so that no two vertices share the same color.
- Stability number: The stability number of a graph $G$ is the cardinality of the largest stable set.
- Stable set : Stable set of $\mathbf{G}$ is a subset of the vertices such that no two of them are connected by an edge.


## Interpreting graph solution to real life problem

- By identifying the chromatic number to the graph we can solve the storage problem by partition the warehouse into a number equals to the chromatic number.
- For assigning compartment number to chemicals can be done by special property independent set.


## Graph coloring

The chromatic number for this graph is 3 . So the warehouse should be partitioned into three compartments for storage


Assign F, D - compartment 1
B, C, E - compartment 2
A - compartment 3

| Compartments | Vertices |
| :---: | :---: |
| 1 | B C E |
| 2 | A |
| 3 |  |

## References

- https://www.case.edu/ehs/ChemSafety/compatC omplex.pdf
- http://ijcem.in/wp-content/uploads/2014/05/A-study-of-Vertex-Edge-Coloring-Techniques-withApplication.pdf
- http://www.iro.umontreal.ca/~hahn/IFT3545/GTWA. pdf

Any questions ???????

