

## Variants of Turing Machine (intro) • There are alternative definitions of Turing machines, including versions with multiple tapes or with non-determinism. • They are called *variants* of the Turing machine model. • The original model and all its reasonable variants have the same power - they recognize the same class of languages. • In this section we describe some of these variants and the proofs of equivalence in power. Simplest equivalent "generalized" model • In basic definition, the head can move to the left or right after each step: it cannot stay put. • If we allow the head to stay put. The transition function would then have the form $\delta: Q \times \Gamma \to Q \times \Gamma \times \{L, R, S\}.$ • Does this make the model more powerful? Might this feature allow Turing machines to recognize additional fanguages? • Of course not. We can replace each stay put transition with two transitions, one that moves to the right and the second back to the left. Theory of Computation, Feodor F. Dragan, Kent State University







Non-deterministic Turing Machine
• A <i>non-deterministic TM</i> is defined in the expected way: at any point of computation the machine may proceed according to several possibilities.
• The transition function for a non-deterministic TM has the form
$\delta: Q \times \Gamma \to \mathbf{P}(Q \times \Gamma \times \{L, R\}).$
• The computation of a non-deterministic TM <i>N</i> is a tree whose branches correspond to different possibilities for the machine.
• Each node of the tree is a configuration of <i>N</i> . The root is the start configuration.
• If some branch of the computation leads to the accept state, the machine accepts the input.
• We will show that non-determinism does not affect the power of the Turing machine model.
• <i>Theorem:</i> Every non-deterministic Turing machine has an equivalent deterministic Turing Machine.
• We show that we can simulate any non-deterministic TM N with a deterministic TM D.
• The idea: <i>D</i> will try all possible branches of <i>N</i> 's non-deterministic computation.
• The TM <i>D</i> searches the tree for an accepting configuration. If <i>D</i> ever finds an accepting configuration, it accepts. Otherwise, <i>D</i> 's simulation will not terminate.
Theory of Computation, Feodor F. Dragan, Kent State University





## Equivalence with other models

• We have presented several variants of the Turing Machines and have proved them to be equivalent in power.

• Many other models of general purpose computation have been proposed in literature.

• Some of these models are very much like Turing machines, while others are quite different (e.g.  $\lambda$  -calculus).

• All share the essential feature of Turing machines, namely, *unrestricted access to unlimited memory*, distinguishing them from weaker models such us finite automata and pushdown automata.

• All models with that feature turn out to be equivalent in power, so long as they satisfy certain reasonable requirements (e.g., the ability to perform only a finite amount of work in a single step).

## More variants of Turing machine

- *k*-PDA, a PDA with *k* stacks.
- write-once Turing machines.
- Turing machines with doubly infinite tape.
- Turing machines with left reset
- Turing machines with stay put instead of left

 $\delta: Q \times \Gamma \to Q \times \Gamma \times \{R, RESET\}.$  $\delta: Q \times \Gamma \to Q \times \Gamma \times \{R, S\}.$ 

• If you missed a HW, try to give a complete answer to *one* of the problems 3.9, 3.11 – 3.14. Only *one* and *complete* answer will be accepted. Then you will get 10 points extra credit. Theory of Computation, Feodor F. Dragan, Kent State University 9