From Physical Clocks to Logical Clocks

- Physical clocks (last time)
 - With a receiver, a clock can be synchronized to within 0.1–10 ms of UTC
 - On a network, computer clocks can be synchronized to within 30 ms of each other (using NTP)
 - Quartz crystal clocks drift 1 µs per second (1 ms per 16.6 minutes)
 - In 30 ms, a 100 MIPS machine can execute 3 million instructions
 - We will refer to these clocks as physical clocks, and say they measure global time
- Idea abandon idea of physical time
 - For many purposes, it is sufficient to know the order in which events occurred
 - Lamport (1978) introduce logical (virtual) time, synchronize logical clocks

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Events and Event Ordering

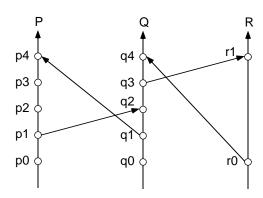
- For many purposes, it is sufficient to know the <u>order</u> in which two events occurred
 - An event may be an instruction execution, may be a function execution, etc.
 - Events include message send / receive
- Within a single process, or between two processes on the same computer,
 - the order in which two events occur can be determined using the physical clock
- Between two different computers in a distributed system,
 - the order in which two events occur cannot be determined using local physical clocks, since those clocks cannot be synchronized perfectly

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The "Happened Before" Relation

- Lamport defined the happened before relation (denoted as "→"), which describes a causal ordering of events:
 - if a and b are events in the same process, and a occurred before b, then a→b
 - (2) if a is the event of sending a message m in one process, and b is the event of receiving that message m in another process, then $a \rightarrow b$
 - (3) if $a \rightarrow b$, and $b \rightarrow c$, then $a \rightarrow c$ (i.e., the relation " \rightarrow " is transitive
- Causality:
 - Past events influence future events
 - This influence among causally related events (those that can be ordered by "→") is referred to as causal affects
 - If $a \rightarrow b$, event a causally affects event b

The "Happened Before" Relation (cont.)



- Concurrent events;
 - Two distinct events a and b are said to be concurrent (denoted "a || b"), if neither a→b nor b→a
 - In other words, concurrent events do not causally affect each other
- For any two events a and b in a system, either: $a \rightarrow b$ or $b \rightarrow a$ or $a \parallel b$

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Lamport's Logical Clocks

- To implement "→" in a distributed system, Lamport (1978) introduced the concept of logical clocks, which captures "→" numerically
- Each process P_i has a logical clock C_i
- Clock C_i can assign a value C_i (a) to any event a in process P_i
 - The value C_i (a) is called the timestamp of event a in process P_i
 - The value C(a) is called the timestamp of event a in whatever process it occurred
- The timestamps have no relation to physical time, which leads to the term *logical clock*
 - The logical clocks assign monotonically increasing timestamps, and can be implemented by simple counters

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Conditions Satisfied by the Logical Clocks

- Clock condition: if $a \rightarrow b$, then C(a) < C(b)
 - If event a happens before event b, then the clock value (timestamp) of a should be less than the clock value of b
 - Note that we can **not** say: if C(a)<C(b), then a→b
- Correctness conditions (must be satisfied by the logical clocks to meet the clock condition above):
 - [C1] For any two events a and b in the same process P_i , if a happens before b, then $C_i(a) < C_i(b)$
 - [C2] If event a is the event of sending a message m in process P_i , and event b is the event of receiving that same message m in a different process P_k , then $C_i(a) < C_k(b)$

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Implementation of Logical Clocks

- Implementation Rules (guarantee that the logical clocks satisfy the correctness conditions):
 - [IR1] Clock C_i must be incremented between any two successive events in process P_i :

$$C_i := C_i + d$$
 (d >0) (usually d =1)

[IR2] If event a is the event of sending a message m in process P_i , then message m is assigned a timestamp $t_m = C_i(a)$

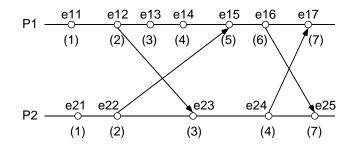
When that same message m is received by a different process P_k , C_k is set to a value greater than or equal to its present value, and greater than t_m :

$$C_k := \max(C_k, t_m + d)$$

($d > 0$) (usually $d = 1$)

Example of Logical Clocks

Updating logical clocks using Lamport's method:



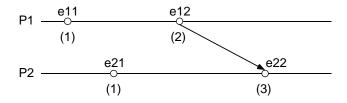
"enn" is event; "(n)" is clock value

■ Notes:

- Clocks initially 0, d=1
- Most clocks incremented due to IR1
- Sends e12, e22, e16, and e24 use IR1
- Receives e23, e15, and e17 set to C_{ν}
- Receive e25 sets to $t_m + d = 6 + 1 = 7$

Obtaining a Total Ordering Using Logical Clocks

■ The happened before relationship "→" defines an irreflexive partial order among events



- A **total order** of events ("⇒") can be obtained as follows:
 - If a is any event in process P_i, and b is any event in process P_k, then a ⇒b if and only if either:

$$C_i(a) < C_k(b)$$
 or $C_i(a) = C_k(b)$ and $P_i << P_k$

where "<<" denotes a relation that totally orders the processes to break ties

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Vector Clocks

- Independently proposed by Fidge and by Mattern in 1988
- Vector clocks:

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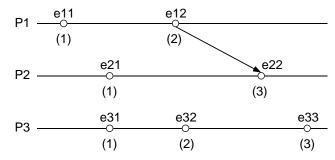
- Assume system contains n processes
- Each process P_i has a clock C_i, which is an integer vector of length n

$$C_i = (C_i[1], C_i[2], \dots C_i[n])$$

- C_i(a) is the timestamp (clock value) of event a at process P_i
- C_i[i](a), entry i of of C_i, is P_i's logical time
- $C_i[k](a)$, entry k of of C_i (where $k \neq i$), is P_i 's best guess of the logical time at P_k
 - More specifically, the time of the occurrence of the last event in P_k which "happened before" the current event in P_i (based on messages received)

Limitation of Logical Clocks

- With Lamport's logical clocks, if $a \rightarrow b$, then C(a) < C(b)
 - The following is **not** necessarily true if events a and b occur in different processes: if C(a) < C(b), then a→b
- Example illustrating this limitation:



- C(e11) < C(e22), and $e11 \rightarrow e22$ is true
- C(e11) < C(e32), but $e11 \rightarrow e32$ is false
- → Cannot determine whether two evens are causally related from timestamps

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Implementation of Vector Clocks

■ Implementation Rules:

[IR1] Clock C_i must be incremented between any two successive events in process P_i :

$$C_i[i] := C_i[i] + d$$
 (*d*>0, usually *d*=1)

[IR2] If event a is the event of sending a message m in process P_i , then message m is assigned a vector timestamp $t_m = C_i(a)$

When that same message m is received by a different process P_k , C_k is updated as follows:

 $\forall p, C_k[p] := \max(C_k[p], t_m[p] + d)$ (usually d=0 unless needed to model network delay)

■ It can be shown that $\forall i, \forall k : C_i[i] \geq C_k[i]$

Implementation of Vector Clocks (cont.)

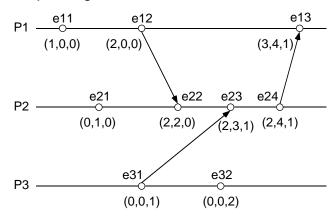
- Rules for comparing timestamps can also be established so that if $t_a < t_b$, then $a \rightarrow b$
 - $t_a = t_b$ iff for all i, $t_a[i] = t_b[i]$
 - $t_a \ll t_b$ iff for any i, $t_a[i] \ll t_b[i]$
 - $t_a <= t_b$ iff for all i, $t_a[i] <= t_b[i]$ (each one equal or less)
 - $t_a < t_b$ iff $t_a <= t_b$ and $t_a <> t_b$ (some (but not all) equal, some less)
 - Solves the problem with Lamport's clocks

■ Examples:

- \bullet 1 1 2 3 = 1 1 2 3
- 1123<>1124
- 1123 <= 1124 1123 <= 1123</p>
- 1123<1124</p>

Example of Vector Clocks

Updating vector clocks:



"enn" is event; "(n,n,n)" is clock value

■ Notes:

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- Events e11, e21, and e12 updated by IR1
- Receive e22 updated by IR1 and IR2
- Receive e13 tells P1 about P2 and P3 (P3 clock is old, but better than nothing!)

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