#### From Physical Clocks to Logical Clocks

- Physical clocks (last time)
  - With a receiver, a clock can be synchronized to within 0.1–10 ms of UTC
  - On a network, computer clocks can be synchronized to within 30 ms of each other (using NTP)
  - Quartz crystal clocks drift 1 µs per second (1 ms per 16.6 minutes)
  - In 30 ms, a 100 MIPS machine can execute 3 million instructions
  - We will refer to these clocks as *physical clocks*, and say they measure *global* time
- Idea abandon idea of physical time
  - For many purposes, it is sufficient to know the <u>order</u> in which events occurred
  - Lamport (1978) introduce logical (virtual) time, synchronize logical clocks

### The "Happened Before" Relation

- Lamport defined the *happened before* relation (denoted as "→"), which describes a **causal ordering** of events:
  - if a and b are events in the same process, and a occurred before b, then a→b
  - (2) if *a* is the event of sending a message *m* in one process, and *b* is the event of receiving that message *m* in another process, then *a*→*b*
  - (3) if  $a \rightarrow b$ , and  $b \rightarrow c$ , then  $a \rightarrow c$  (i.e., the relation " $\rightarrow$ " is transitive
- Causality:

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- Past events influence future events
- This influence among causally related events (those that can be ordered by "→") is referred to a *causal affects*
- If  $a \rightarrow b$ , event a causally affects event b

## **Events and Event Ordering**

- For many purposes, it is sufficient to know the <u>order</u> in which two events occurred
  - An event may be an instruction execution, may be a function execution, etc.
  - Events include message send / receive
- Within a single process, or between two processes on the same computer,
  - the order in which two events occur **can** be determined using the physical clock
- Between two different computers in a distributed system,
  - the order in which two events occur cannot be determined using local physical clocks, since those clocks cannot be synchronized perfectly

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# The "Happened Before" Relation (cont.)



Concurrent events;

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- Two distinct events a and b are said to be concurrent (denoted "a ∥ b"), if neither a→b nor b→a
- In other words, concurrent events do not causally affect each other
- For any two events *a* and *b* in a system, either:  $a \rightarrow b$  or  $b \rightarrow a$  or  $a \parallel b$

## Lamport's Logical Clocks

- To implement "→" in a distributed system, Lamport (1978) introduced the concept of logical clocks, which captures "→" numerically
- Each process *P<sub>i</sub>* has a *logical clock C<sub>i</sub>*
- Clock C<sub>i</sub> can assign a value C<sub>i</sub> (a) to any event a in process P<sub>i</sub>
  - The value *C<sub>i</sub>* (*a*) is called the *timestamp* of event *a* in process *P<sub>i</sub>*
  - The value *C*(*a*) is called the *timestamp* of event *a* in whatever process it occurred
- The timestamps have no relation to physical time, which leads to the term logical clock
  - The logical clocks assign monotonically increasing timestamps, and can be implemented by simple counters

#### Implementation of Logical Clocks

- Implementation Rules (guarantee that the logical clocks satisfy the correctness conditions):
  - [IR1] Clock  $C_i$  must be incremented between any two successive events in process  $P_i$ :

 $C_i := C_i + d$  (*d*>0) (usually *d*=1)

[IR2] If event *a* is the event of sending a message *m* in process  $P_i$ , then message *m* is assigned a timestamp  $t_m = C_i(a)$ 

> When that same message *m* is received by a different process  $P_k$ ,  $C_k$  is set to a value greater than or equal to its present value, and greater than  $t_m$ :

$$C_k := \max(C_k, t_m + d)$$
(d>0) (usually d=1)

#### Conditions Satisfied by the Logical Clocks

- Clock condition: if  $a \rightarrow b$ , then C(a) < C(b)
  - If event a happens before event b, then the clock value (timestamp) of a should be less than the clock value of b
  - Note that we can **not** say: if C(a) < C(b), then  $a \rightarrow b$
- Correctness conditions (must be satisfied by the logical clocks to meet the clock condition above):
  - [C1] For any two events *a* and *b* in the same process  $P_i$ , if *a* happens before *b*, then  $C_i(a) < C_i(b)$
  - [C2] If event *a* is the event of sending a message *m* in process  $P_i$ , and event *b* is the event of receiving that same message *m* in a <u>different</u> <u>process</u>  $P_k$ , then  $C_i(a) < C_k(b)$

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#### **Example of Logical Clocks**

Updating logical clocks using Lamport's method:



"enn" is event; "(n)" is clock value

Notes:

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- Clocks initially 0, d=1
- Most clocks incremented due to IR1
- Sends e12, e22, e16, and e24 use IR1
- Receives e23, e15, and e17 set to  $C_k$
- Receive e25 sets to  $t_m + d = 6 + 1 = 7$

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#### Obtaining a Total Ordering Using Logical Clocks

■ The happened before relationship "→" defines an irreflexive partial order among events



- A total order of events ("⇒") can be obtained as follows:
  - If *a* is any event in process  $P_i$ , and *b* is any event in process  $P_k$ , then  $a \Rightarrow b$  if and only if either:
    - $C_i(a) < C_k(b)$  or

$$C_i(a) = C_k(b)$$
 and  $P_i << P_k$ 

where "<<" denotes a relation that totally orders the processes to break ties

#### **Vector Clocks**

- Independently proposed by Fidge and by Mattern in 1988
- Vector clocks:
  - Assume system contains *n* processes
  - Each process *P<sub>i</sub>* has a clock *C<sub>i</sub>*, which is an integer vector of length *n*

 $C_i = (C_i[1], C_i[2], \dots C_i[n])$ 

- *C<sub>i</sub>(a)* is the timestamp (clock value) of event *a* at process *P<sub>i</sub>*
- C<sub>i</sub>[i](a), entry i of of C<sub>i</sub>, is P<sub>i</sub>'s logical time
- C<sub>i</sub>[k](a), entry k of of C<sub>i</sub> (where k≠i), is
   P<sub>i</sub>'s best guess of the logical time at P<sub>k</sub>
  - More specifically, the time of the occurrence of the last event in P<sub>k</sub> which "happened before" the current event in P<sub>i</sub> (based on messages received)

## **Limitation of Logical Clocks**

- With Lamport's logical clocks, if  $a \rightarrow b$ , then C(a) < C(b)
  - The following is **not** necessarily true if events *a* and *b* occur in different processes: if C(a) < C(b), then a→b</li>
- Example illustrating this limitation:



#### Implementation of Vector Clocks

### Implementation Rules:

[IR1] Clock  $C_i$  must be incremented between any two successive events in process  $P_i$ :

 $C_i[i] := C_i[i] + d$  (*d*>0, usually *d*=1)

[IR2] If event *a* is the event of sending a message *m* in process  $P_i$ , then message *m* is assigned a <u>vector</u> timestamp  $t_m = C_i(a)$ 

> When that same message m is received by a different process  $P_k$ ,  $C_k$  is updated as follows:

 $\forall p, C_k[p] := \max(C_k[p], t_m[p] + d)$ (usually d=0 unless needed to model network delay)

It can be shown that  $\forall i, \forall k : C_i[i] \ge C_k[i]$ 

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# Implementation of Vector Clocks (cont.)

- Rules for comparing timestamps can also be established so that if  $t_a < t_b$ , then  $a \rightarrow b$ 
  - $t_a = t_b$  iff for all i,  $t_a[i] = t_b[i]$
  - $t_a \iff t_b$  iff for any i,  $t_a[i] \iff t_b[i]$
  - *t<sub>a</sub>* <= *t<sub>b</sub>* iff for all i, *t<sub>a</sub>*[i] <= *t<sub>b</sub>*[i] (each one equal or less)
  - *t<sub>a</sub>* < *t<sub>b</sub>* iff *t<sub>a</sub>* <= *t<sub>b</sub>* and *t<sub>a</sub>* <> *t<sub>b</sub>* (some (but not all) equal, some less)
  - Solves the problem with Lamport's clocks
- Examples:

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- 1 1 2 3 = 1 1 2 3
- 1 1 2 3 <> 1 1 2 4
- 1 1 2 3 <= 1 1 2 4 1 1 2 3 <= 1 1 2 3

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• 1 1 2 3 < 1 1 2 4

