

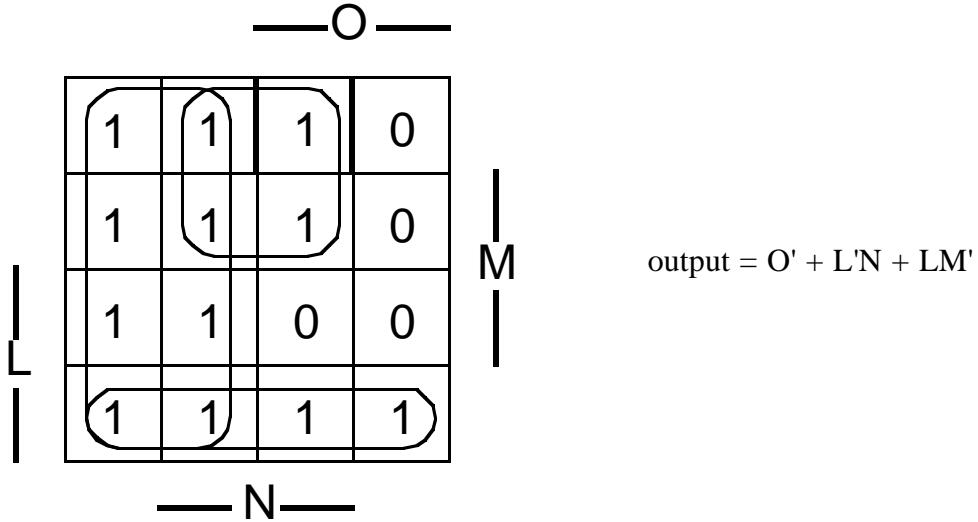
Monday 21 September 1998

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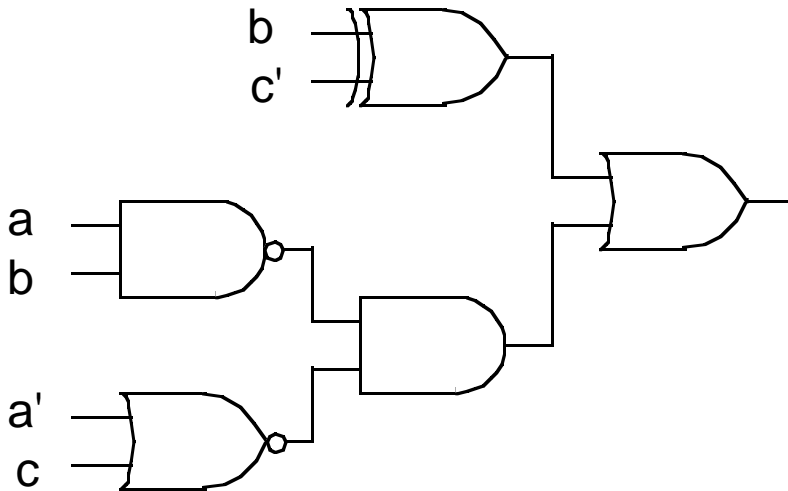
1. For each of the following statements, write the word “true” below the statement if it is true, and “false” below the statement if it is false. (5 points each = 20 points)
- a. Mechanical adding machines usually have more significant digits than slide rules.
- True
- b. Mechanical adding machines can use logarithms to multiply and divide.
- False
- c. Early computers were used to compute artillery tables during World War II.
- True
- d. Before becoming president of IBM, Thomas Watson was a highly successful stockbroker.
- False
2. Give the truth table for a combinational circuit that takes a two-bit input labeled  $A_1A_0$  and a two-bit input labeled  $B_1B_0$  and produces a one-bit output  $C$  that is true (1) if the value  $A_1A_0$  is numerically *greater than* the value  $B_1B_0$  and is false (0) otherwise. (15 points)

A1	A0	B1	B0	C
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	0

3. Given the Karnaugh Map below, draw the appropriate ovals on the map, and write the simplified two-level sum-of-products expression to the right of the map. (20 points)



4. Draw the combinational circuit that *directly* corresponds to the Boolean equation  $z = (b \oplus c') + (ab)'(a'+c)'$  in the space below. (20 points)



Name: \_\_\_\_\_

**5. Perform the following conversions, showing your work. (5 points each = 15 points)**

**a.  $29_{10}$  to base 2**

$$29/2 = 14, \text{ rem } 1$$

$$14/2 = 7, \text{ rem } 0$$

$$7/2 = 3, \text{ rem } 1$$

$$3/2 = 1, \text{ rem } 1$$

$$1/2 = 0, \text{ rem } 1$$

the answer is  $11101_2$

**b.  $1100010101_2$  to base 8**

$$1100010101$$

$$= \underline{001} \ 100 \ 010 \ 101 \text{ (adding two leading zeros)}$$

with 3 digits per octal digit,

the answer is  $1425_8$

**c.  $15A_{16}$  to base 10**

(note that  $A = 10$ )

$$1 \cdot 16^2 + 5 \cdot 16 + 10$$

$$= 256 + 80 + 10$$

the answer is  $346_{10}$

**6. This question explores the difference between different types of encoding. (5 points each = 10 points)**

**a. Does it require more or less bits to store “23” as a ASCII character string than as a number? Explain your answer.**

It would probably require more bits. Storing “23” as an ASCII string would require 7 bits for each character, for a total of 14 bits (or 16 bits, if each character is stored in a separate byte). Storing “23” as a number would require at least 5 bits (“23” is “10111” in binary) (or 8 bits if it is stored in a single byte). Either way, the numerical representation is smaller.

**b. What is the basic idea behind Huffman encoding? (Note — I’m not asking for the entire algorithm or a detailed example, just the basic idea.)**

Analyze the frequency with which the characters to be encoded occur, and use less bits than average for frequently-occurring characters, and more bits than average for seldom-occurring characters.