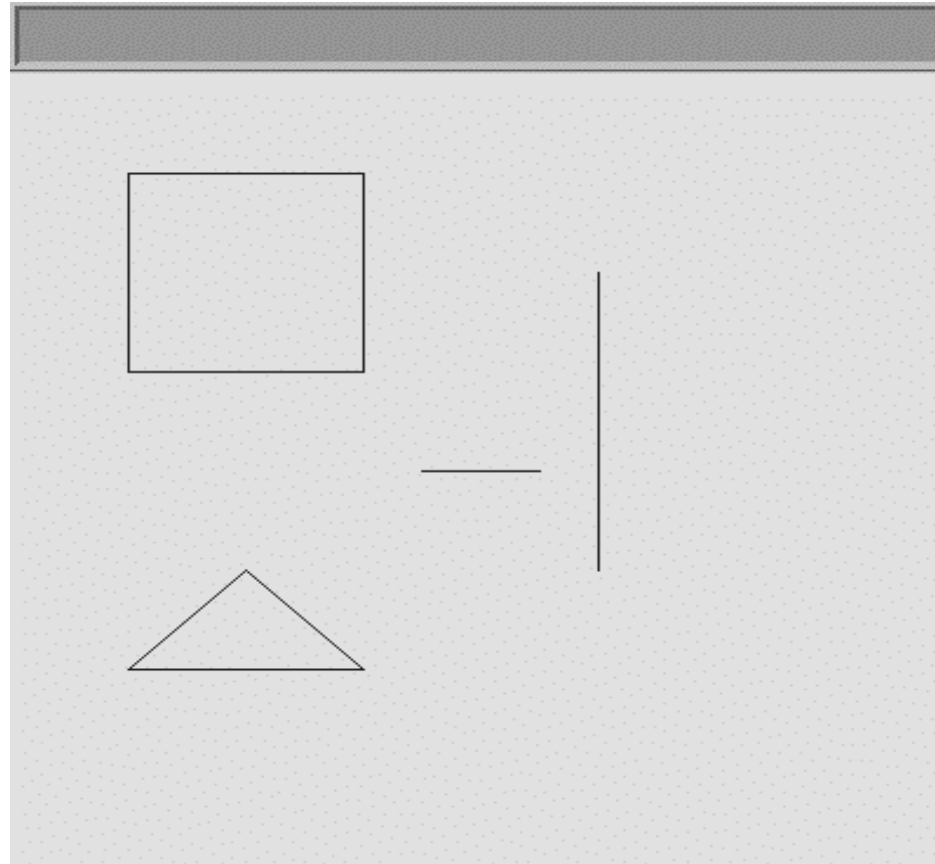


Rendering

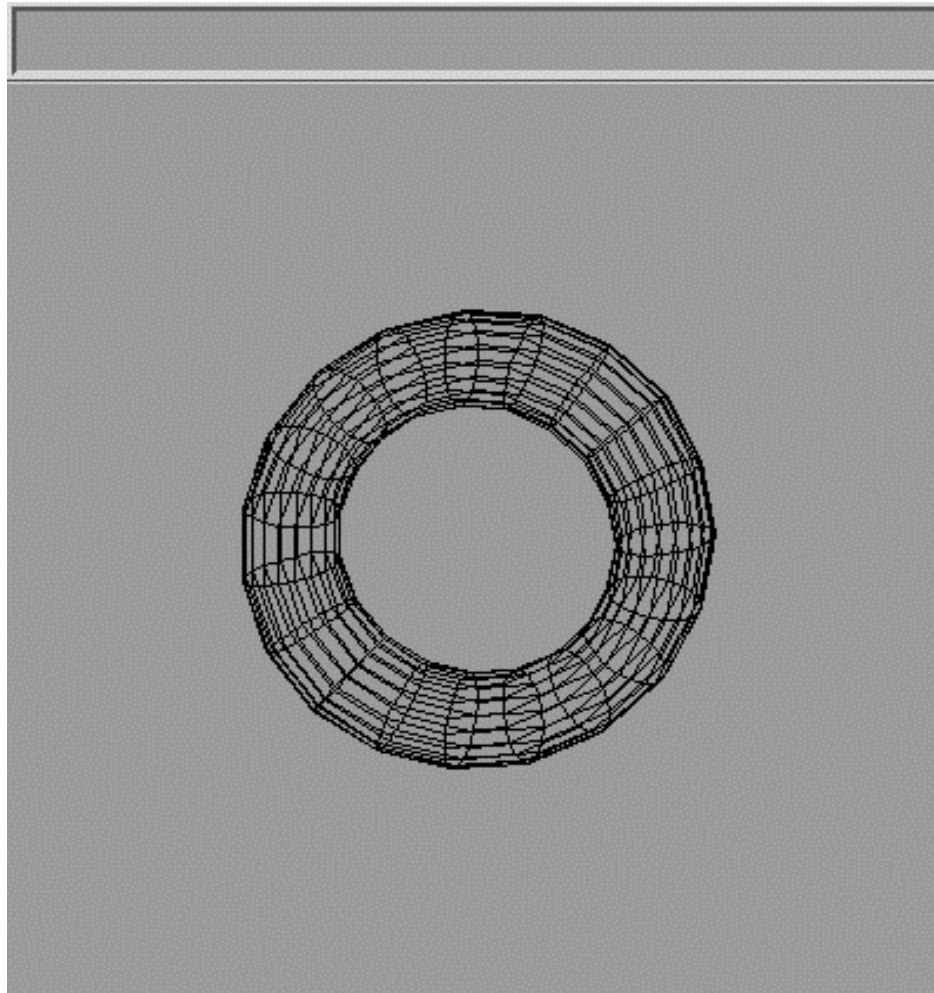


- **A simple X program to illustrate rendering**
- The programs in this directory provide a simple x based application for us to develop some graphics routines.
- Please notice the following:
 - All points are integers.
 - The line drawing algorithm is very simple and has some definite flaws.

A simple X program



A simple X program



Syntax

■ Point

■ point x y where x and y are integers

■ Line

■ line x1 y1 x2 y2

■ where x1, x2, y1 and y2 are integers

Point and line drawing routines



- These are the *primitives* in the simple package!!
- Point drawing routines
 - point.c
 - point.h
- Line drawing routines
 - line.c
 - line.h

Other routines



- The main routine
 - main.c
- Include file with the definitions of the data structures
 - mygraph.h
- The routines to Access X functions directly.
 - Xroutines.c
 - Xroutines.h

Line Drawing and Scan Conversion

- A preliminary step to drawing lines is choosing a suitable representation for them.
- There are three possible choices which are potentially useful.
- Explicit: $y = f(x)$
 - $y = m(x - x_0) + y_0$ where $m = dy/dx$
- Parametric: $x = f(t), y = f(t)$
 - $x = x_0 + t(x_1 - x_0), t \text{ in } [0,1]$
 - $y = y_0 + t(y_1 - y_0)$

Point and line drawing routines (ctd)

- Implicit: $f(x,y) = 0$
 - $F(x,y) = (x-x_0)dy - (y-y_0)dx$
 - if $F(x,y) = 0$ then (x,y) is on line
 - $F(x,y) > 0$ then (x,y) is below line
 - $F(x,y) < 0$ then (x,y) is above line

Rasterization or Scan Conversion



- Drawing lines on a raster grid implicitly involves approximation.
- The general process : *rasterization* or *scan-conversion*.
- What is the best way to draw a line from the pixel (x_1, y_1) to (x_2, y_2) ?
- Such a line should ideally have the following properties.
 - straight
 - pass through endpoints
 - smooth
 - independent of endpoint order
 - uniform brightness
 - brightness independent of slope
 - efficient

Line Drawing - Algorithm 1

A Straightforward Implementation

```
Drawline(x1,y1,x2,y2)
int x1,y1,x2,y2;
{
    float y;
    int x;

    for (x=x1; x<=x2; x++) {
        y = y1 + (x-x1)*(y2-y1)/(x2-x1)
        SetPixel(x, Round(y) );
    }
}
```

Line Drawing - Algorithm 2

A Better Implementation

DrawLine(x1,y1,x2,y2)

int x1,y1,x2,y2;

{

float m,y;

int dx,dy,x;

dx = x2 - x1;

dy = y2 - y1;

m = dy/dx;

y = y1 + 0.5;

for (x=x1; x<=x2; x++) {

SetPixel(x, Floor(y));

y = y + m;

}

}

Line Drawing - Algorithm 2

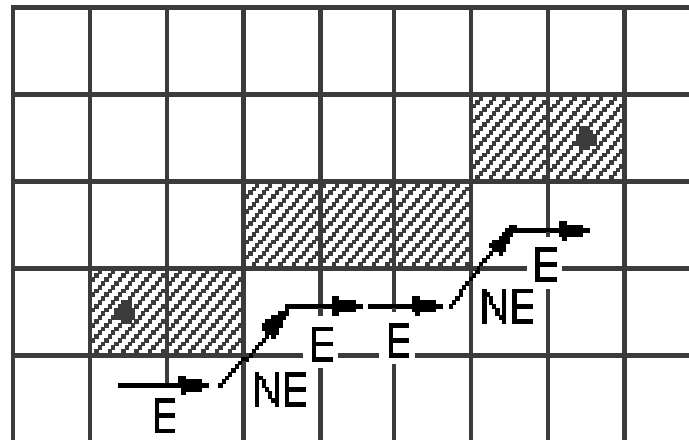


- Advantages over Algorithm 1
 - eliminates multiplication
 - improves speed
- Disadvantages
 - round-off error builds up
 - get pixel drift
 - rounding and floating point arithmetic still time consuming
 - works well only for $|m| < 1$
 - need to loop in y for $|m| > 1$
 - need to handle special cases

Line Drawing - Midpoint Algorithm

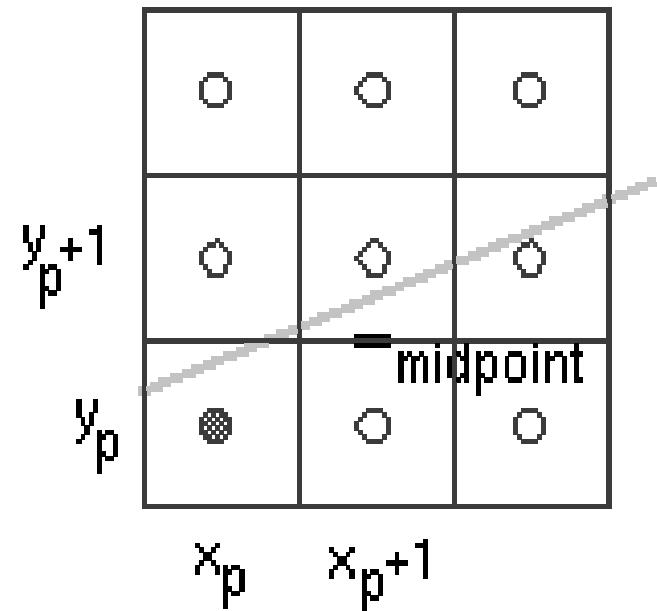
■ The Midpoint or Bresenham's Algorithm

- The midpoint algorithm is even better than the above algorithm in that it uses only integer calculations. It treats line drawing as a sequence of decisions. For each pixel that is drawn the next pixel will be either N or NE, as shown below.



Midpoint Algorithm

- The midpoint algorithm makes use of the implicit definition of the line, $F(x,y) = 0$. The N/NE decisions are made as follows.
- $d = F(x_p + 1, y_p + 0.5)$
 - if $d < 0$ line below midpoint choose E
 - if $d > 0$ line above midpoint choose NE
- if E is chosen
 - $d_{\text{new}} = F(x_p + 2, y_p + 0.5)$
 - $d_{\text{new}} - d_{\text{old}} = F(x_p + 2, y_p + 0.5) - F(x_p + 1, y_p + 0.5)$
 - $\Delta d = d_{\text{new}} - d_{\text{old}} = dy$



Midpoint Algorithm

- If NE is chosen

- $d_{\text{new}} = F(x_p + 2, y_p + 1.5)$

- $\Delta d = dy - dx$

- Initialization

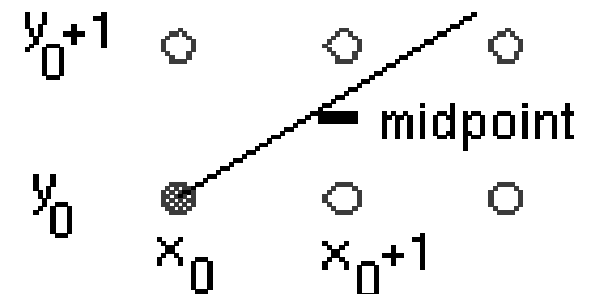
- $d_{\text{start}} = F(x_0 + 1, y_0 + 0.5) = (x_0 + 1 - x_0) dy - (y_0 + 0.5 - y_0) dx$
 $= dy - dx/2$

- Integer only algorithm

- $F'(x,y) = 2 F(x,y) \quad ; \quad d' = 2d$

- $d'_{\text{start}} = 2dy - dx$

- $\Delta d' = 2\Delta d$



Midpoint Algorithm for $x_1 < x_2$ and slope ≤ 1

```
drawline(x1, y1, x2, y2, colour)
int x1, y1, x2, y2, colour;
{
    int dx, dy, d, incE, incNE, x, y;

    dx = x2 - x1;
    dy = y2 - y1;
    d = 2*dy - dx;
    incE = 2*dy;
    incNE = 2*(dy - dx);
    y = y1;
    for (x=x1; x<=x2; x++) {
        setpixel(x, y, colour);
        if (d>0) {
            d = d + incNE;
            y = y + 1;
        } else {
            d = d + incE;
        }
    }
}
```