

Pythagoras discovered that a musical *interval*—two audible frequencies played simultaneously—is *harmonious*—makes a most pleasing sound—if the ratio of the frequencies is a simple fraction. For example, an interval whose frequency ratio is $2/1$ is known as an *octave*. An *equal-tempered chromatic scale* is an increasing geometric series of 13 frequencies, such that the 13th and 1st frequencies form an octave and the ratio of each frequency to the previous one is constant. These days, piano strings are tuned so that pressing 13 successive (black and/or white) keys plays an equal-tempered chromatic scale. Each row in the following table shows a harmonious interval ratio, the name by which musicians refer to the interval, and the two positions in an equal-tempered chromatic scale that approximate the interval:

| ratio | interval name | approximate chromatic |
|-------|----------------|-----------------------|
| | | scale positions |
| 1/1 | unison | 1st and 1st |
| 6/5 | minor third | 4th and 1st |
| 5/4 | major third | 5th and 1st |
| 4/3 | perfect fourth | 6th and 1st |
| 3/2 | perfect fifth | 8th and 1st |
| 8/5 | minor sixth | 9th and 1st |
| 5/3 | major sixth | 10th and 1st |
| 2/1 | octave | 13th and 1st |

This program will compute frequencies in a equal-tempered chromatic scale and the harmonious intervals that they approximate.

Input Format

Each line of the input contains a single positive integer that is the 1st frequency in an equal-tempered chromatic scale.

Output Format

For each line of the input, compute the frequencies in a equal-tempered chromatic scale having the given 1st frequency, and also compute what the 1st, 4th, 5th, 6th, 8th, 9th, 10th and 13th frequencies would be if they formed harmonious Pythagorean intervals with the 1st frequency. Compute all frequencies accurate to four decimal places and format the output as shown in the output sample.

Input and Output Sample

see reverse side of this page

Input Sample

264
440

Output Sample

| equal | pythagorean |
|----------|-------------|
| 264.0000 | 264.0000 |
| 279.6983 | |
| 296.3300 | |
| 313.9507 | 316.8000 |
| 332.6192 | 330.0000 |
| 352.3977 | 352.0000 |
| 373.3524 | |
| 395.5531 | 396.0000 |
| 419.0739 | 422.4000 |
| 443.9933 | 440.0000 |
| 470.3945 | |
| 498.3656 | |
| 528.0000 | 528.0000 |

| equal | pythagorean |
|----------|-------------|
| 440.0000 | 440.0000 |
| 466.1638 | |
| 493.8833 | |
| 523.2511 | 528.0000 |
| 554.3653 | 550.0000 |
| 587.3295 | 586.6667 |
| 622.2540 | |
| 659.2551 | 660.0000 |
| 698.4565 | 704.0000 |
| 739.9888 | 733.3333 |
| 783.9909 | |
| 830.6094 | |
| 880.0000 | 880.0000 |